

M2RI, Parcours Images et Données

Module Acquisition et Représentation des Données

Extraction de caractéristiques

Features Extraction - 2

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Irisa/Insa

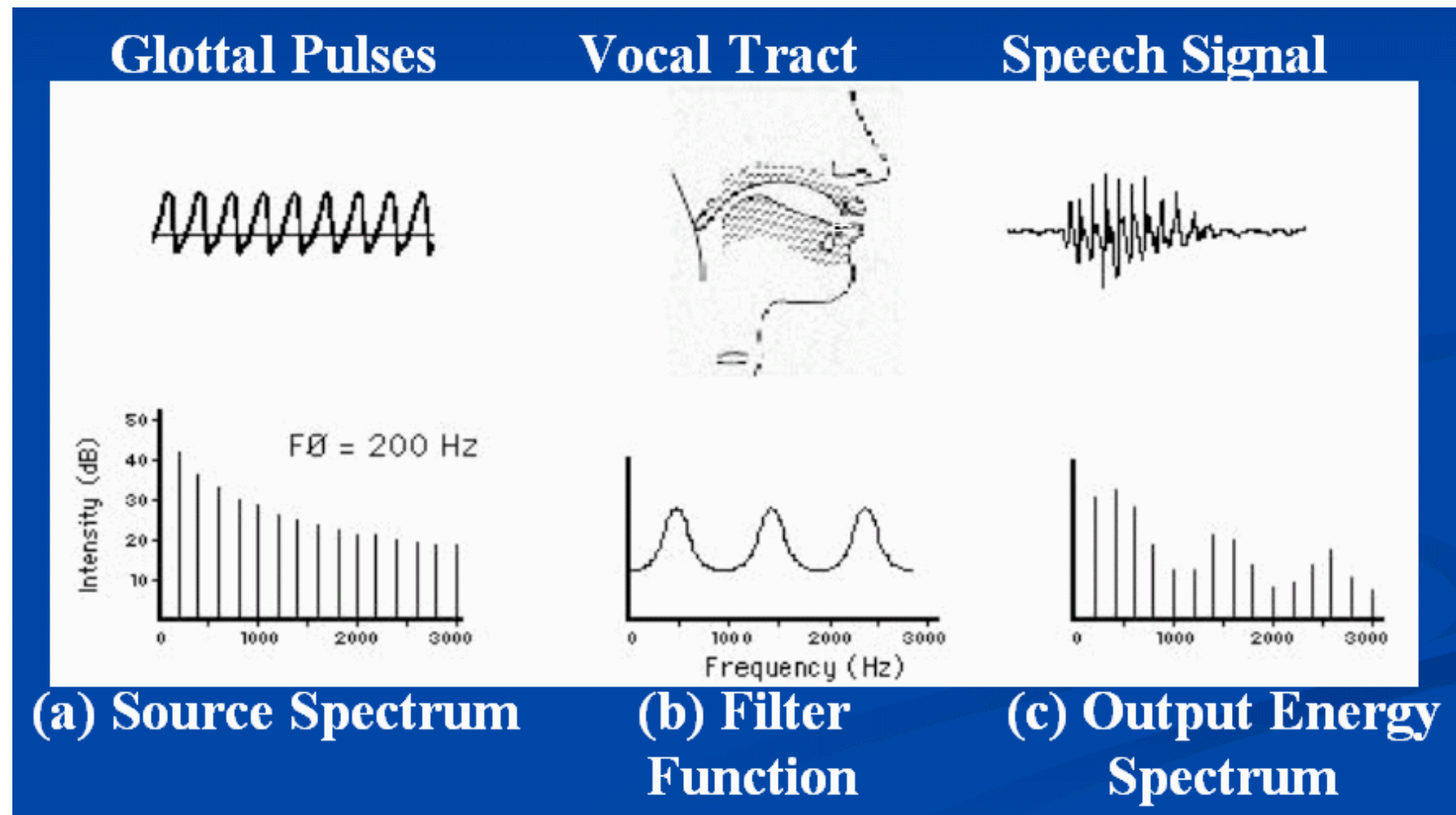
Imadoc

Bureau C314

<http://www.irisa.fr/imadoc>

couasnon@irisa.fr

■ Human speech production



■ Source + filter model

◆ Time model $x(t) = (h \star s)(t)$

◆ Frequency model

$$X(f) = H(f)S(f)$$

$$\log |X(f)| = \log |H(f)| + \log |S(f)|$$

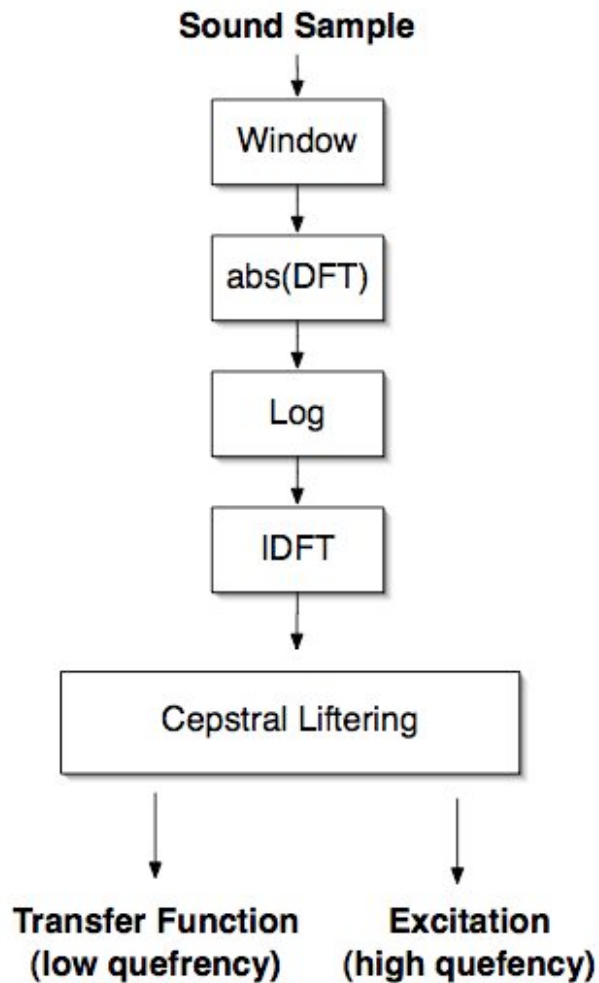
varies slowly varies rapidly

◆ “Quefrequency” model

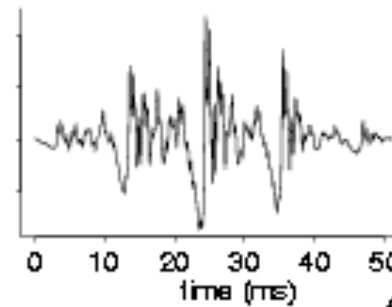
$$F^{-1}\{\log |X(f)|\} = F^{-1}\{\log |H(f)|\} + F^{-1}\{\log |S(f)|\}$$

low quefrequency high quefrequency

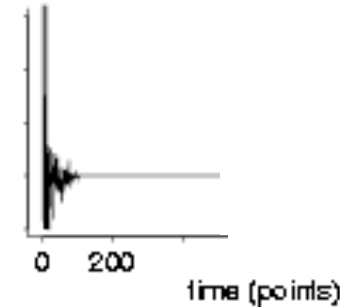
■ Cepstrum



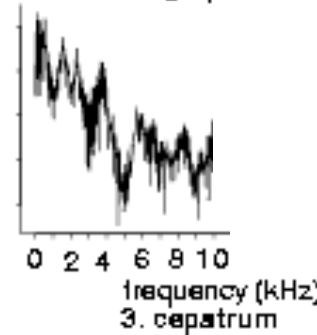
1. hamming-windowed waveform



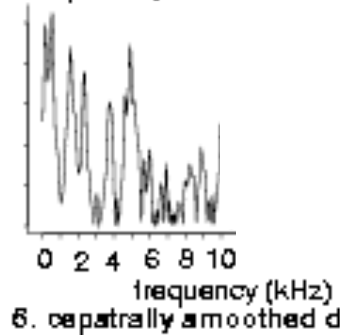
4. windowed cepstrum



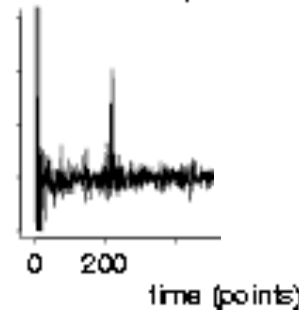
2. log spectrum



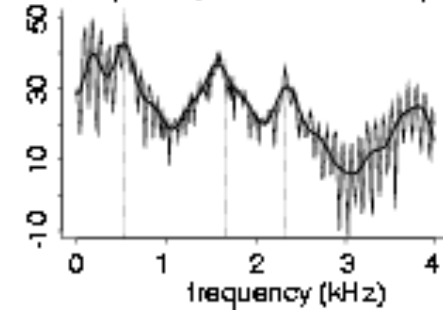
5. cepstrally smoothed log spectrum



3. cepstrum

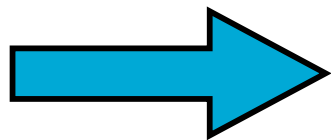


6. cepstrally smoothed dB spectrum



■ Use of the Cepstrum in speech analysis

- ◆ Compute the cepstrum on 20 msec. window frames, every 10 msec.
- ◆ $N=12$ lowest “quefreny” coefficients
- ◆ +1 energy on each frame
- ◆ + first & second time derivatives

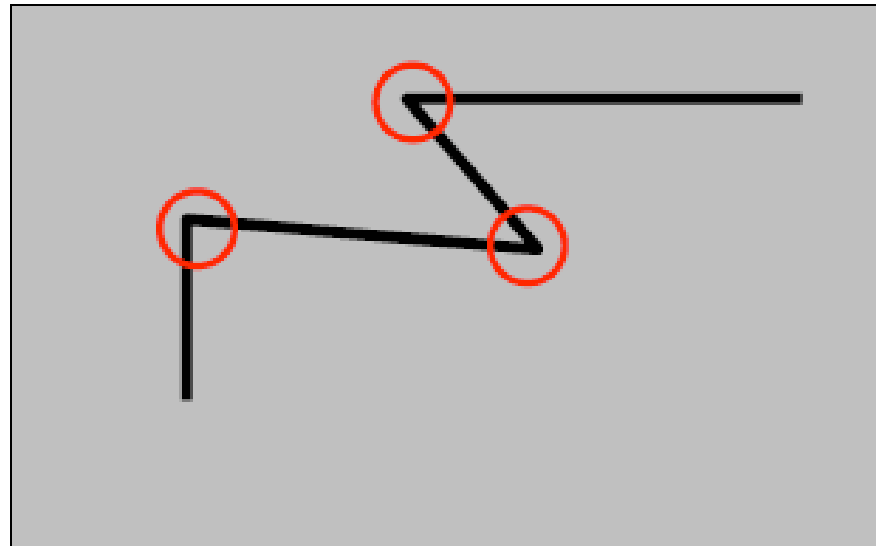


$3(N+1)$ dimensional feature vector
every 10 msec.

- **Difficulties of Feature Extraction**
 - ◆ Segmentation
 - ◆ Recognition in Images
 - ◆ Recognition in Document Images
- **Feature Extraction/Detection on the whole Signal**
 - ◆ Global Descriptor
 - ◆ Local Descriptor
- **Feature Extraction/Detection on Objects**
 - ◆ Object Localization / Extraction
 - ◆ Object Characterization
- **Interest of Multi-Resolution**
- **Using Features**

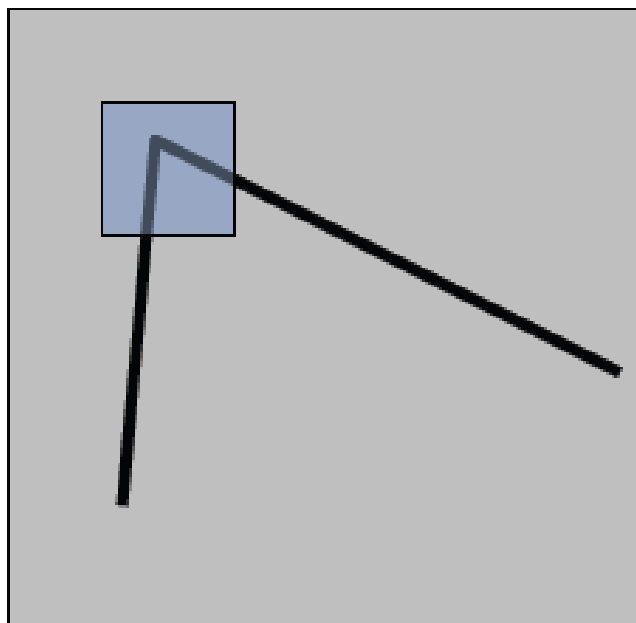
- **Stable across images**
 - ◆ Invariant to small camera transformations
 - ◆ Robust to changes in illumination
- **Descriptive**
 - ◆ Different image patches will be represented differently
 - ◆ Descriptions can be reliably compared
- **Interest Point Detector**
 - ◆ Harris Corner Detector (very popular)
- **Feature Descriptor**
 - ◆ SIFT (best performer)

- Harris corner detector

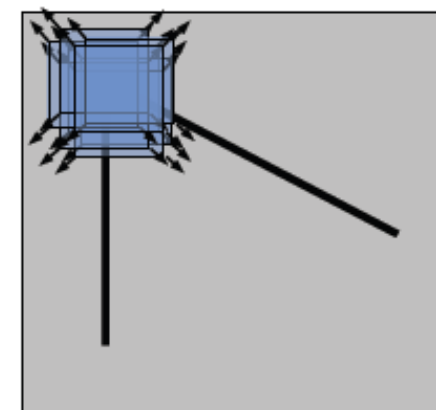
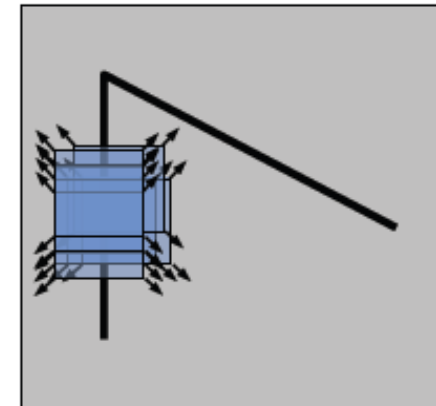
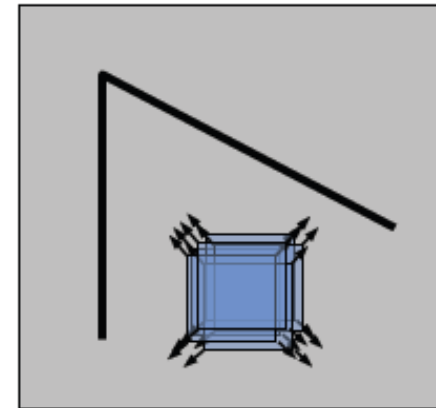


- ◆ C.Harris, M.Stephens. “A Combined Corner and Edge Detector”. 1988

- We should easily recognize the point by looking through a small window
- Shifting a window in any direction should give a large change in intensity



- “flat” region: no change in all directions
- “edge”: no change along the edge direction
- “corner”: significant change in all directions



Change of intensity for the shift $[u, v]$:

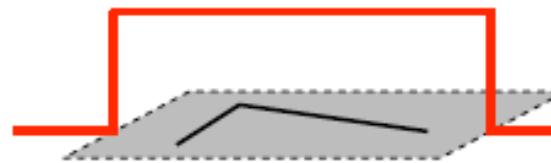
$$E(u, v) = \sum_{x, y} w(x, y) [I(x+u, y+v) - I(x, y)]^2$$

Window
function

Shifted
intensity

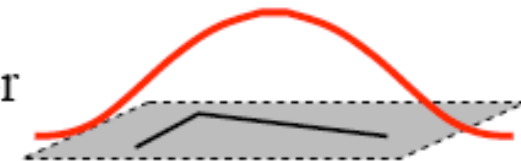
Intensity

Window function $w(x, y) =$



1 in window, 0 outside

or



Gaussian

$$= \sum_{x, y} w(x, y) [I_x u + I_y v + O(u^2, v^2)]^2$$

For small shifts $[u, v]$ we have a *bilinear* approximation:

$$E(u, v) \cong [u, v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

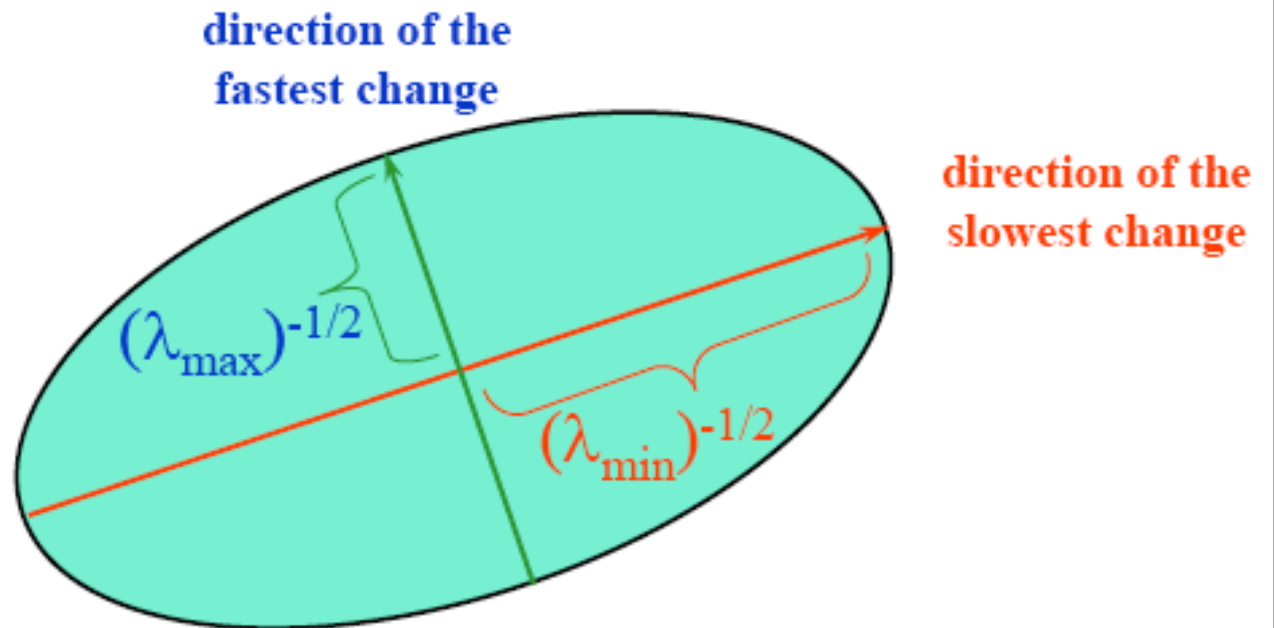
where M is a 2×2 matrix computed from image derivatives:

$$M = \sum_{x, y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

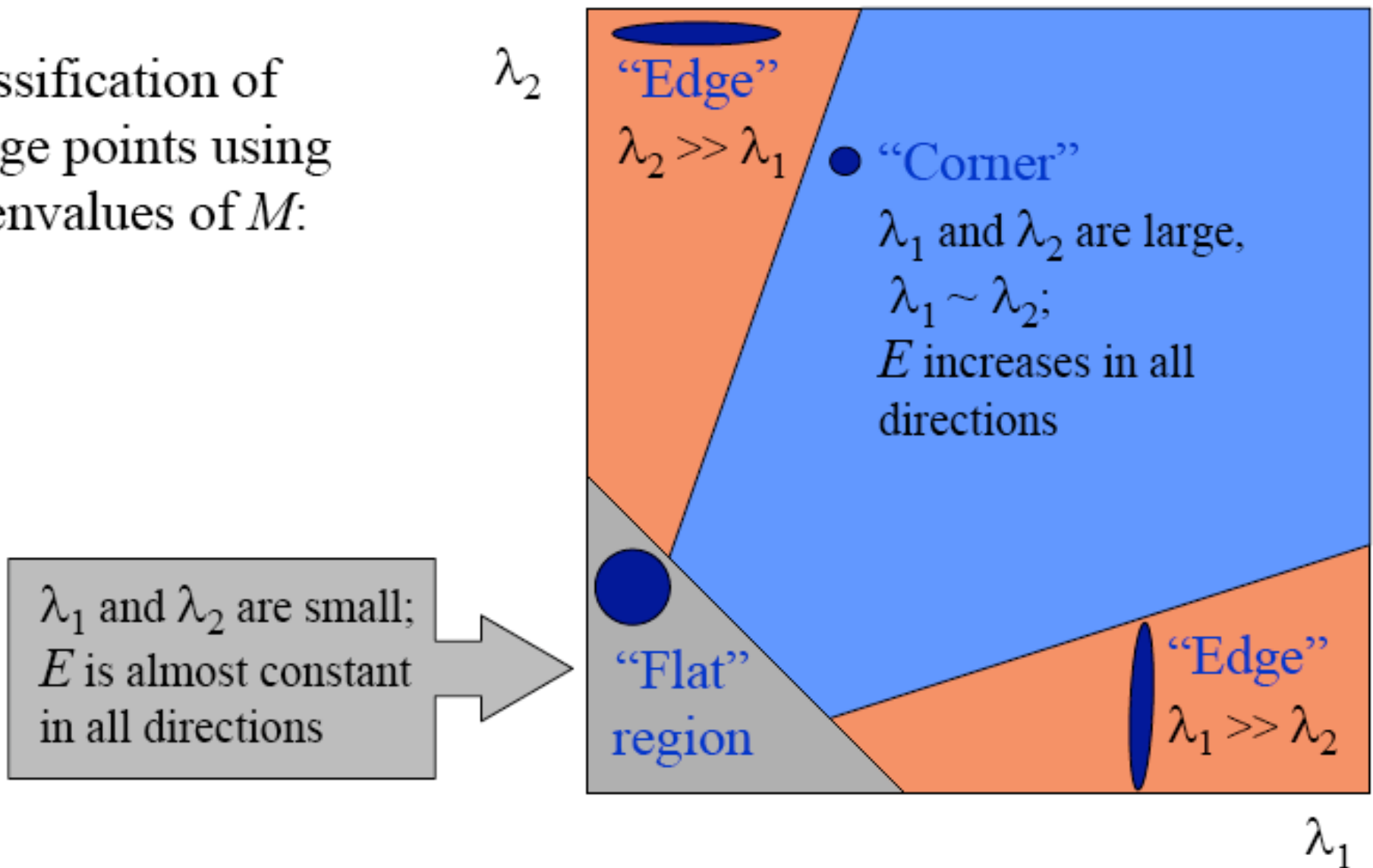
Intensity change in shifting window: eigenvalue analysis

$$E(u, v) \cong [u, v] M \begin{bmatrix} u \\ v \end{bmatrix} \quad \lambda_1, \lambda_2 - \text{eigenvalues of } M$$

Ellipse $E(u, v) = 2$



Classification of image points using eigenvalues of M :



Measure of corner response:

$$R = \det M - k (\text{trace } M)^2$$

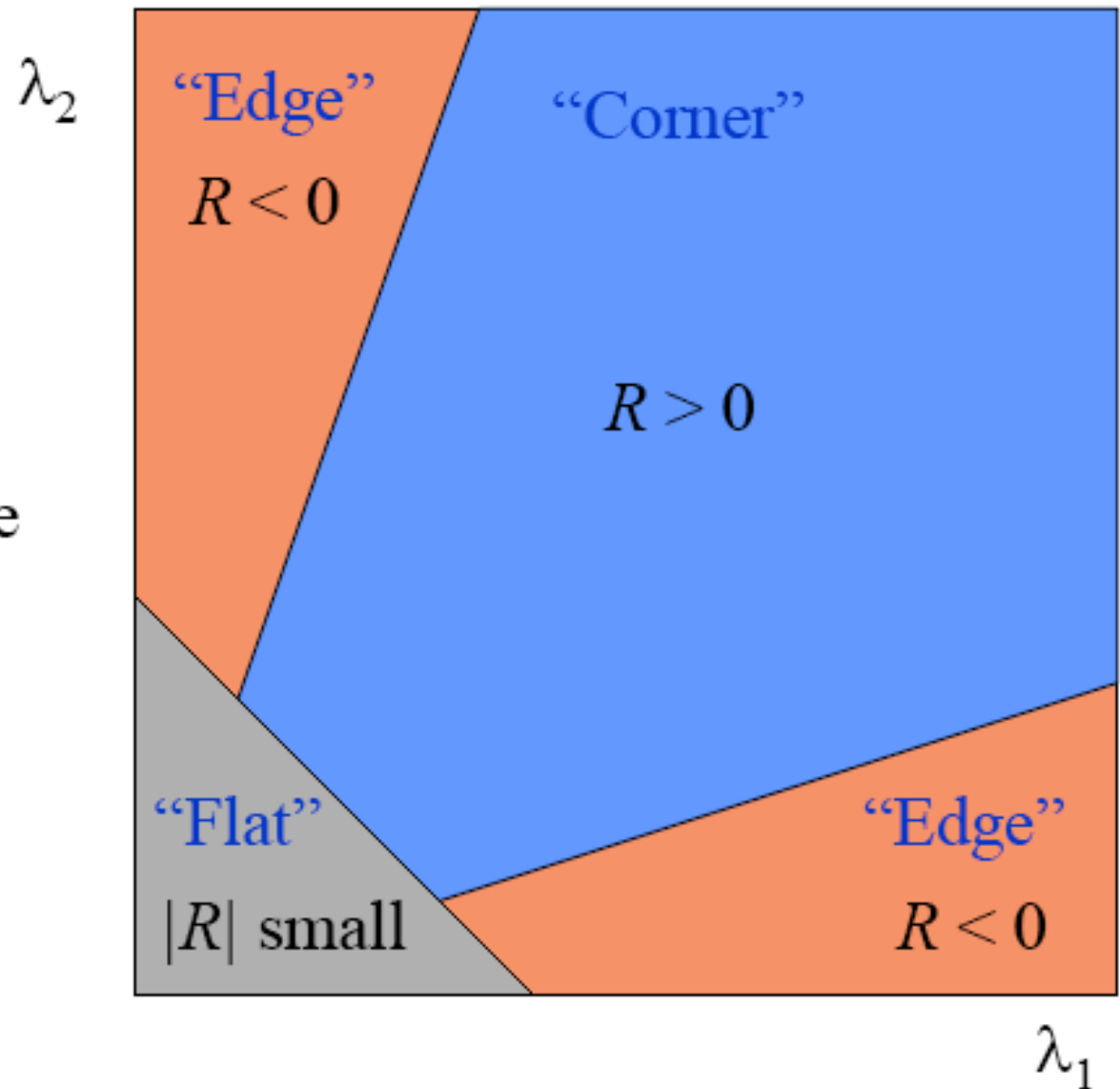
$$\det M = \lambda_1 \lambda_2$$

$$\text{trace } M = \lambda_1 + \lambda_2$$

(k – empirical constant, $k = 0.04-0.06$)

Motivation: computation avoids explicit eigenvalue decomposition

- R depends only on eigenvalues of M
- R is large for a **corner**
- R is negative with large magnitude for an **edge**
- $|R|$ is small for a **flat** region



■ The Algorithm

- ◆ Find points with large corner response function R
($R > \text{threshold}$)
- ◆ Take the points of local maxima of R

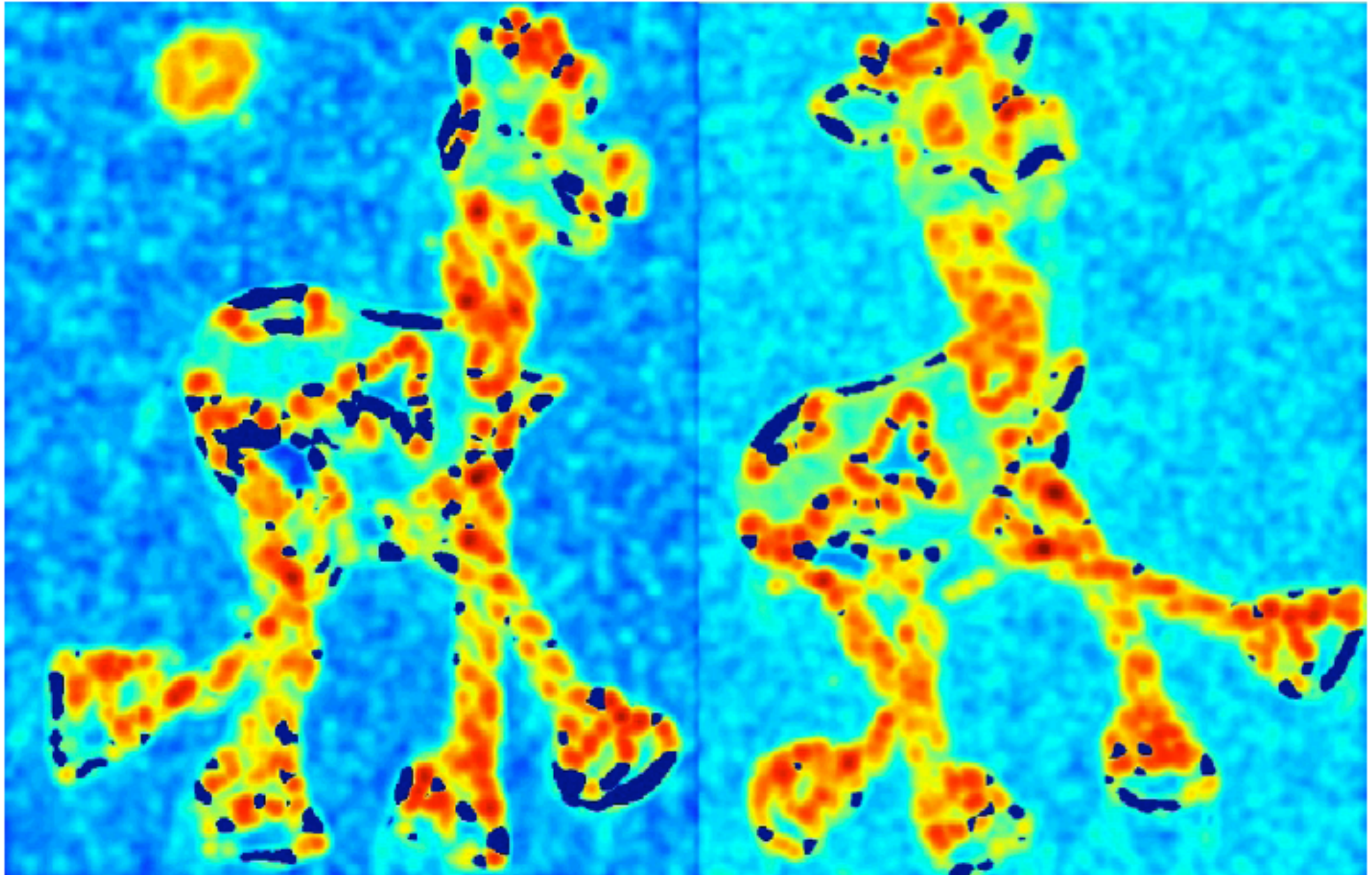
Local Descriptor: Harris - Example

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Local Descriptor: Harris - Example

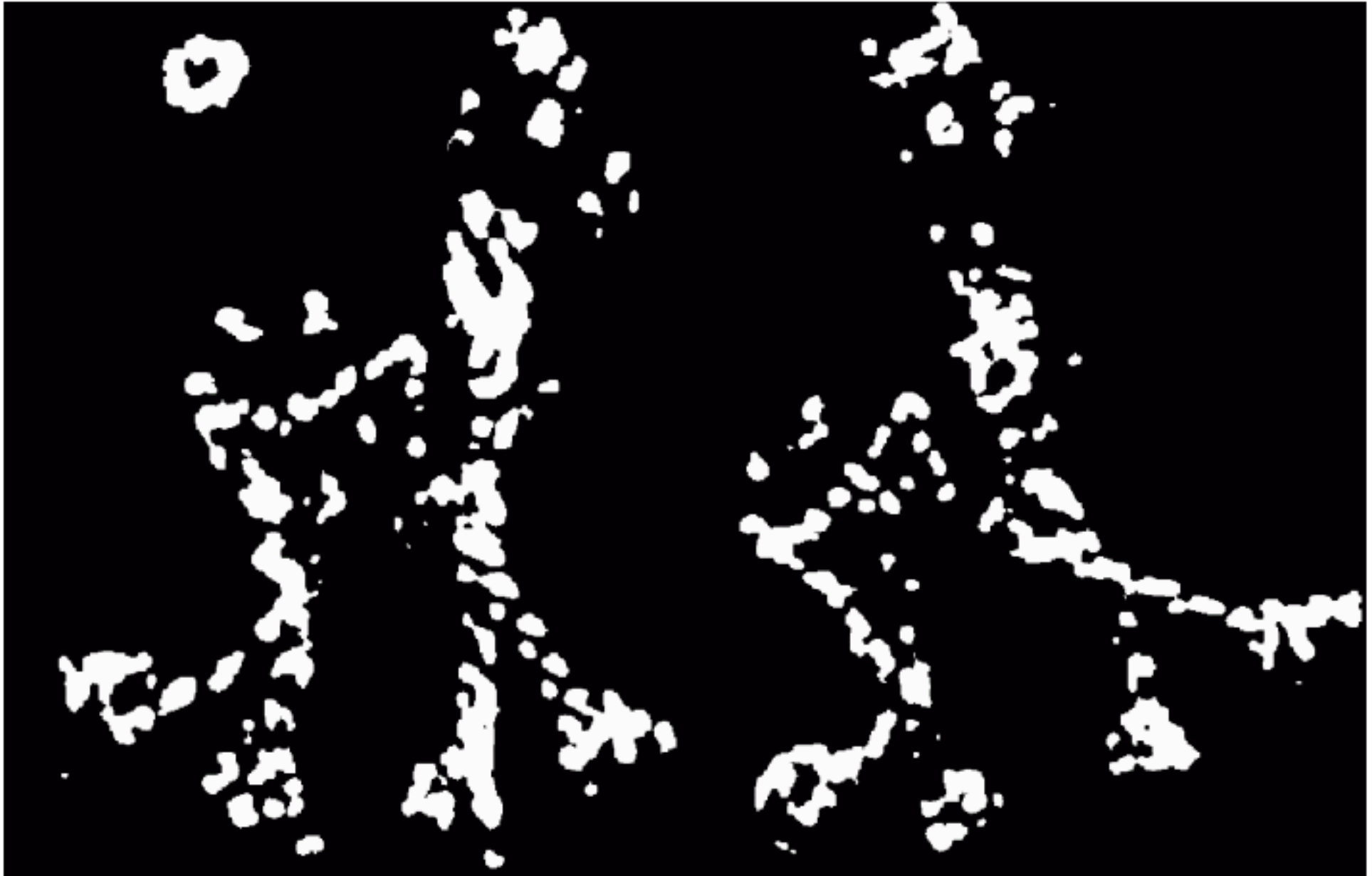
- Compute corner response R



Local Descriptor: Harris - Example

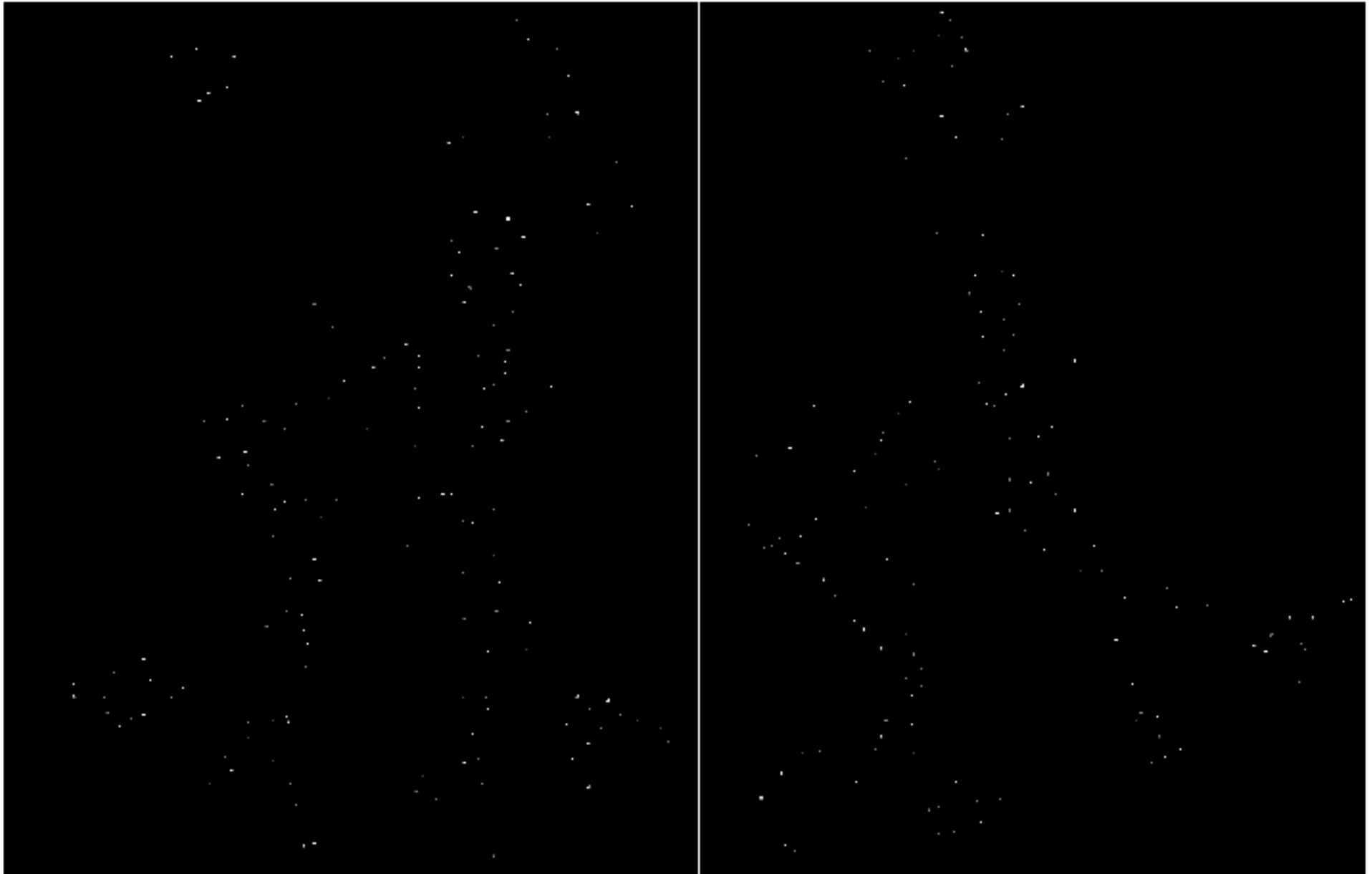
69

- Find points with large corner response: $R > \text{threshold}$



Local Descriptor: Harris - Example

- Take only the points of local maxima of R



Local Descriptor: Harris - Example

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- Average intensity change in direction $[u, v]$ can be expressed as a bilinear form:

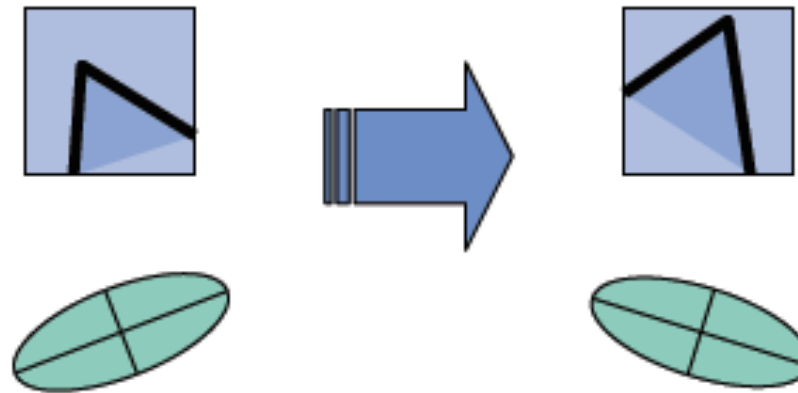
$$E(u, v) \cong [u, v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

- Describe a point in terms of eigenvalues of M :
measure of corner response

$$R = \lambda_1 \lambda_2 - k (\lambda_1 + \lambda_2)^2$$

- A good (corner) point should have a *large intensity change in all directions*, i.e. R should be large and positive

□ Rotation invariance



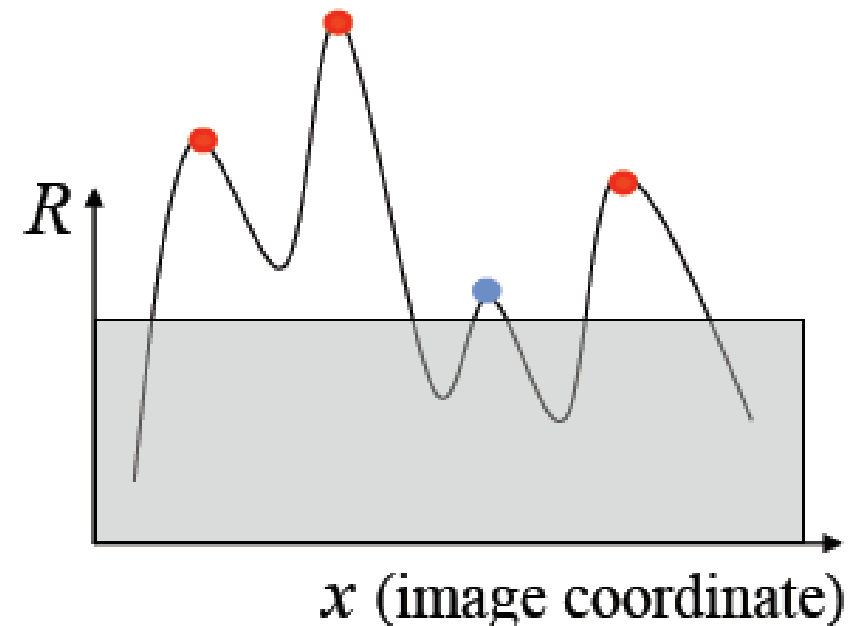
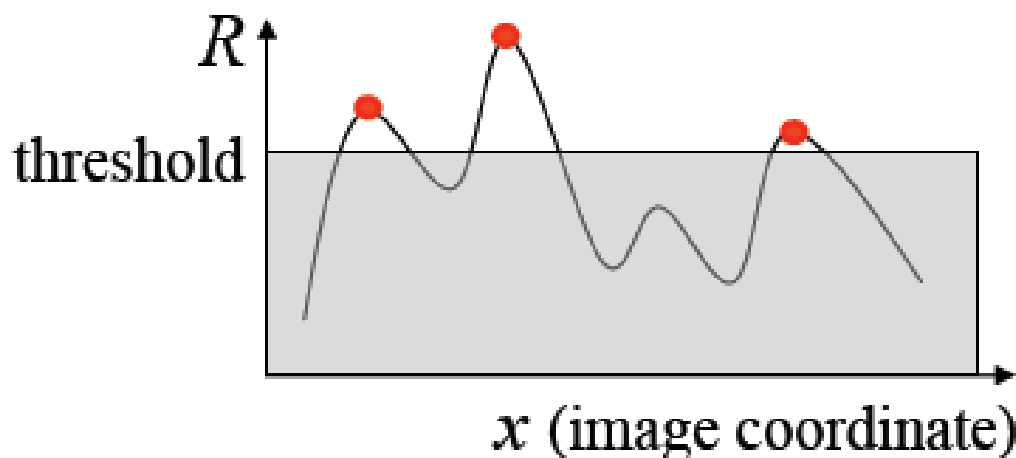
Ellipse rotates but its shape (i.e. eigenvalues) remains the same

Corner response R is invariant to image rotation

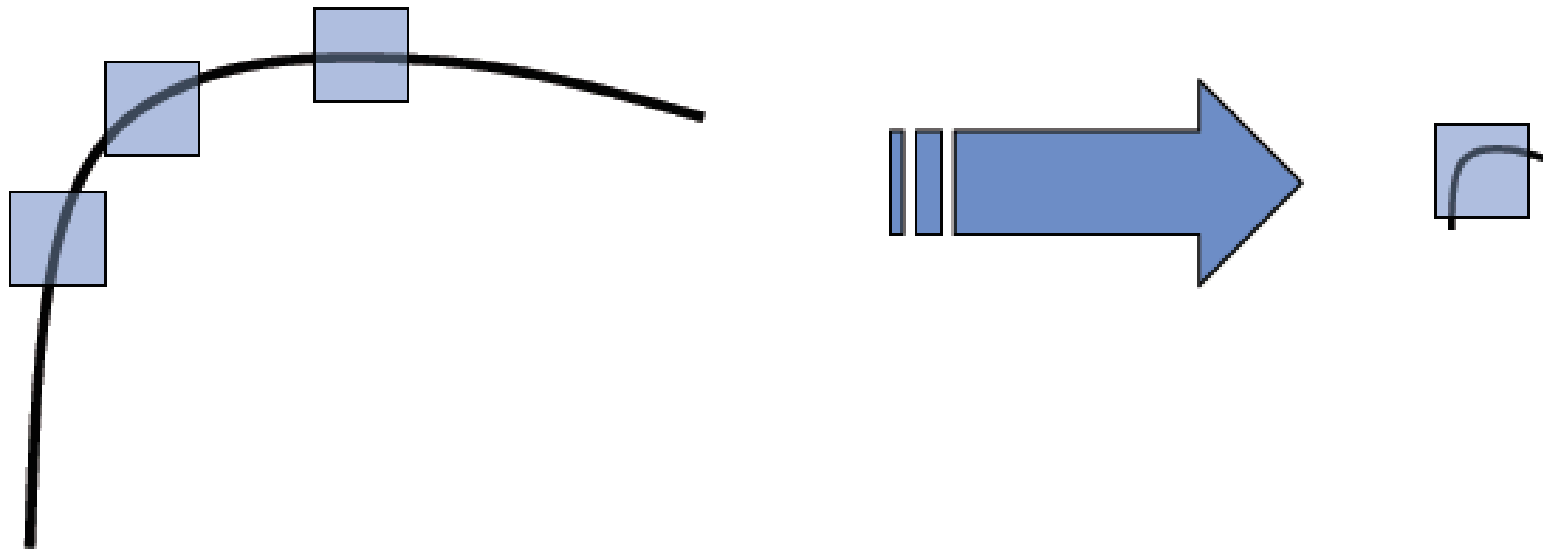
□ Partial invariance to *affine intensity* change

✓ Only derivatives are used \Rightarrow invariance to intensity shift $I \rightarrow I + b$

✓ Intensity scale: $I \rightarrow a I$



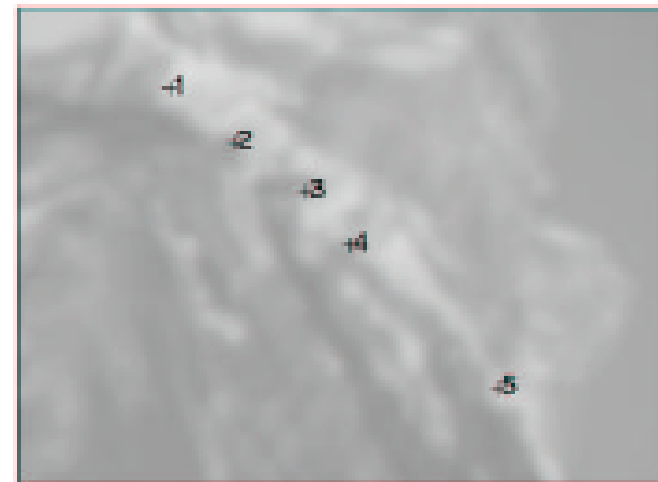
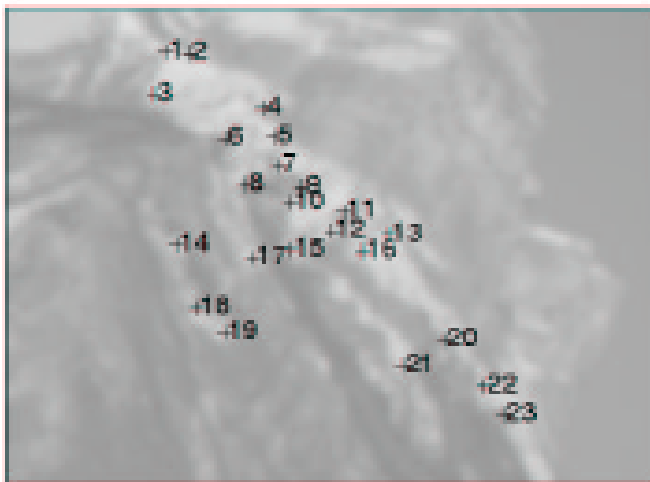
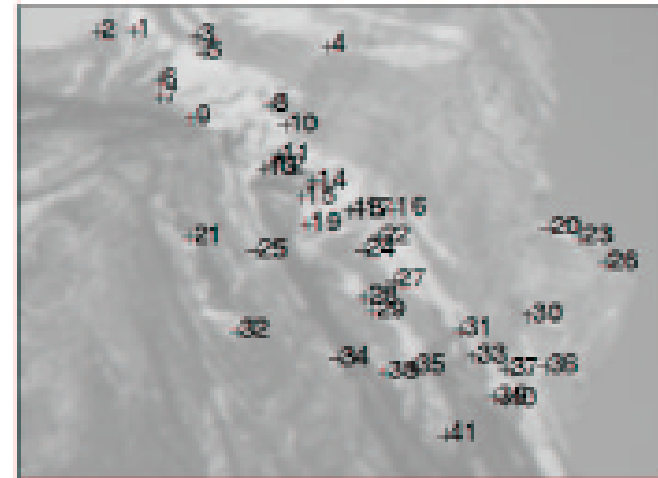
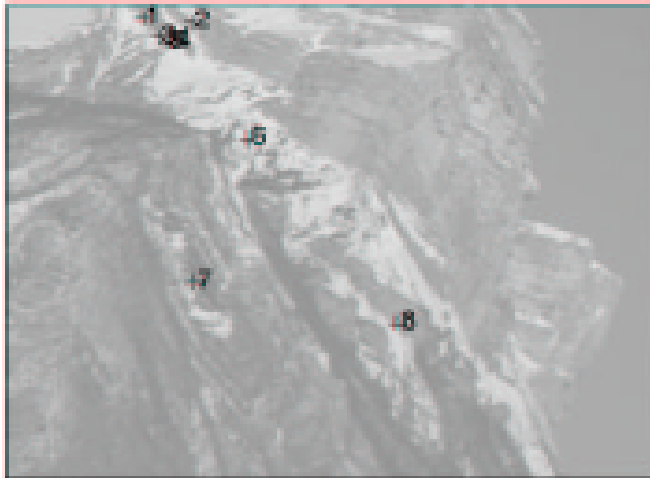
- But: non-invariant to *image scale*!



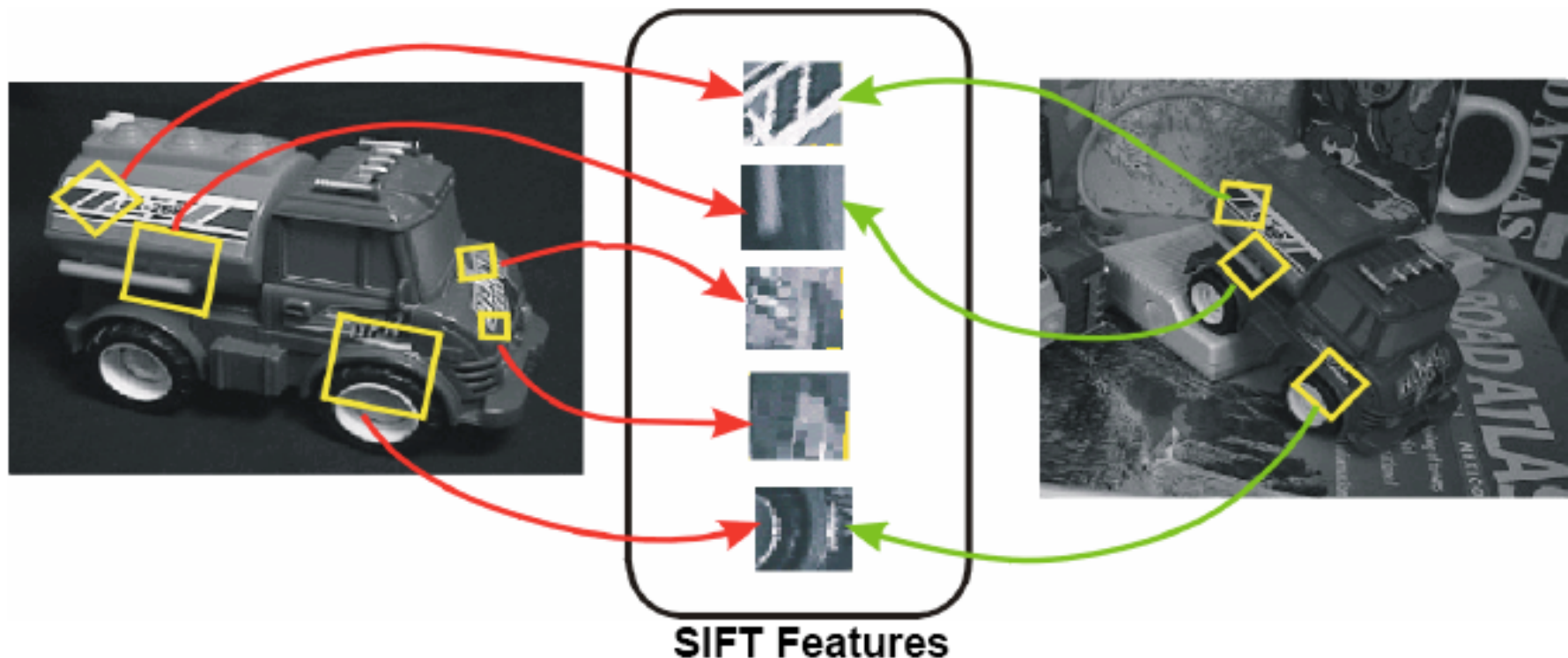
All points will be classified as **edges**

Corner !

■ Example of Harris Corner Detector at different scales



- SIFT: Scale Invariant Feature Transform
- Image content is transformed into local feature coordinates that are invariant to translation, rotation, scale, and other imaging parameters



◆ D.G. Lowe, 1999, 2004

■ 1) Scale-Space Extrema Detection

◆ Interest Point

- ✦ Local extrema of difference-of-Gaussian filters at different scales

■ 2) Keypoint localization

◆ Removes extrema with low contrast

■ 3) Orientation assignment

◆ Gradient Orientation

■ 4) Generation of keypoint descriptors

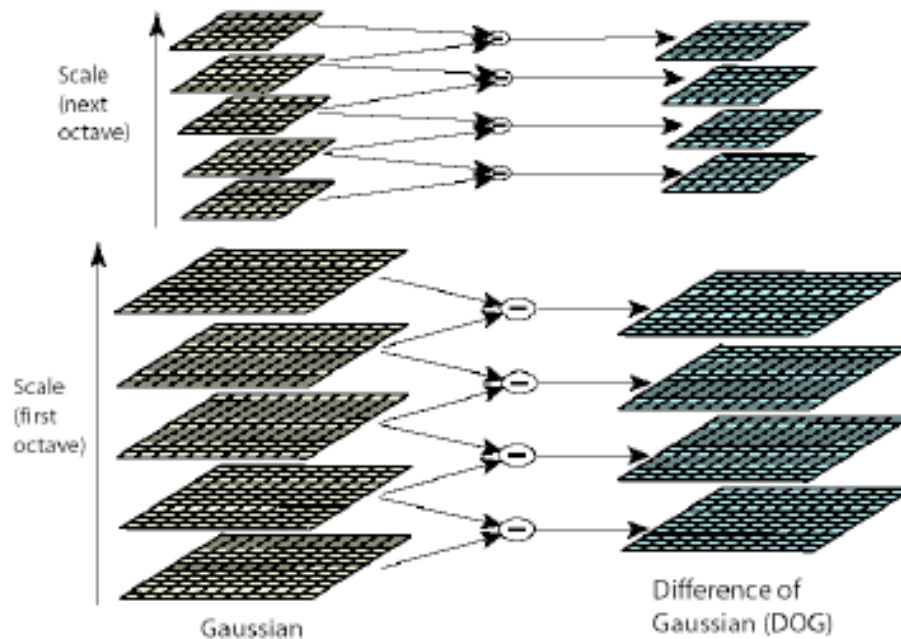
SIFT: 1) Scale-Space Extrema Detection

From Gaussian scale pyramid --

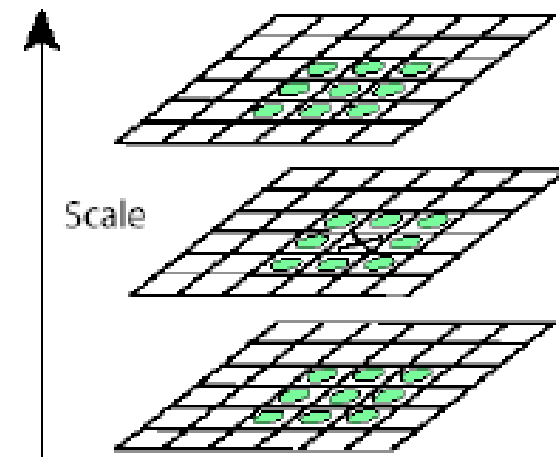
$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

create Difference of Gaussian (DOG) images

$$D(x, y, \sigma) = (G(x, y, k\sigma) - G(x, y, \sigma)) * I(x, y) \\ = L(x, y, k\sigma) - L(x, y, \sigma).$$



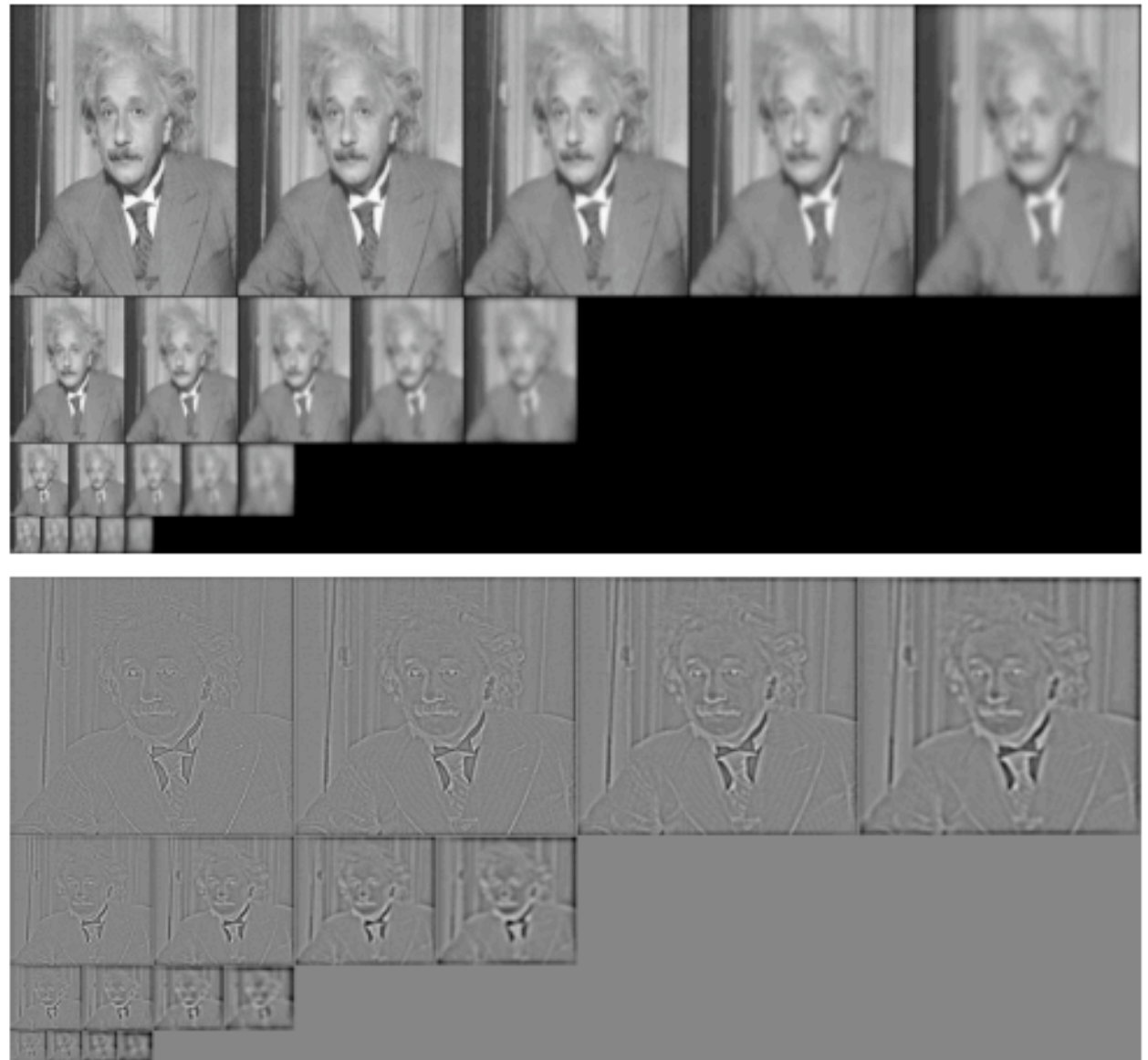
- ◆ Find maximum response over space and scale



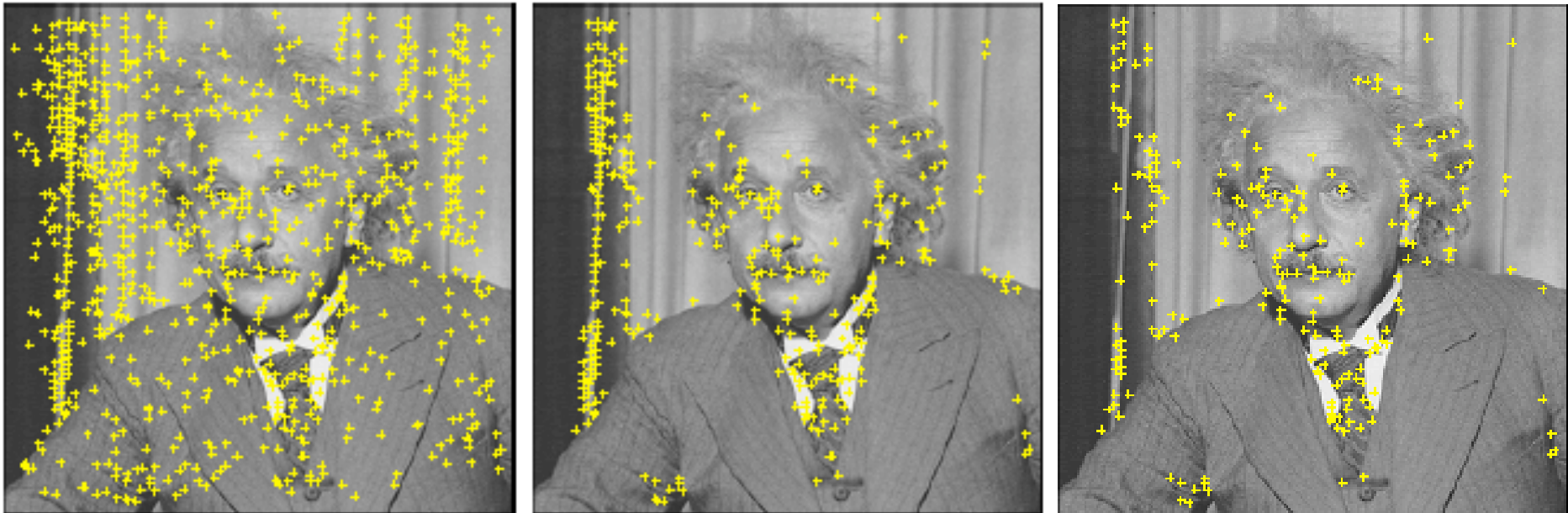
SIFT: 1) Scale-Space Extrema Detection

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- Gaussian blurred images and DoG images grouped by octave



Range: [-0.11, 0.131]
Dims: [959, 2044]



■ 1) Scale-Space Extrema Detection

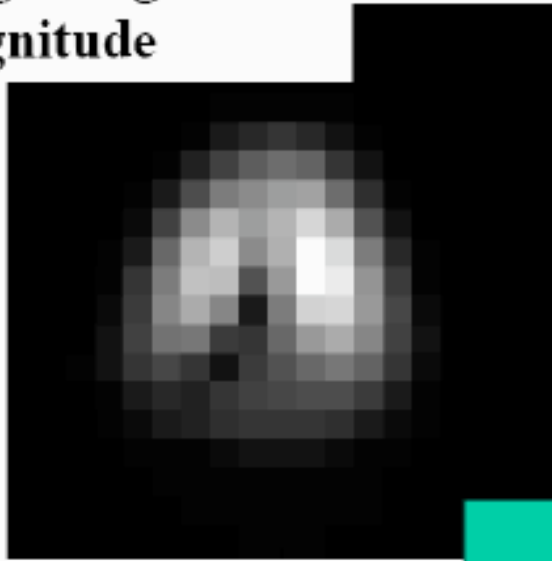
- ◆ Left: Maxima of DoG across scales

■ 2) Keypoint Localization

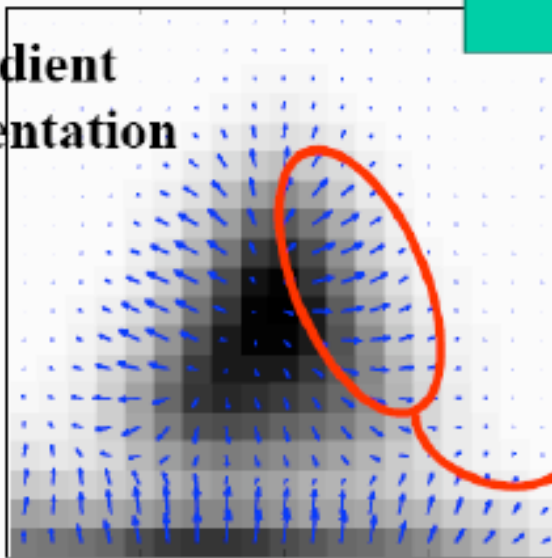
- ◆ Middle: Remaining Keypoint after removal of low contrast point
- ◆ Right: Remaining Keypoint after removal of edge responses

SIFT: 3) Orientation Assignment

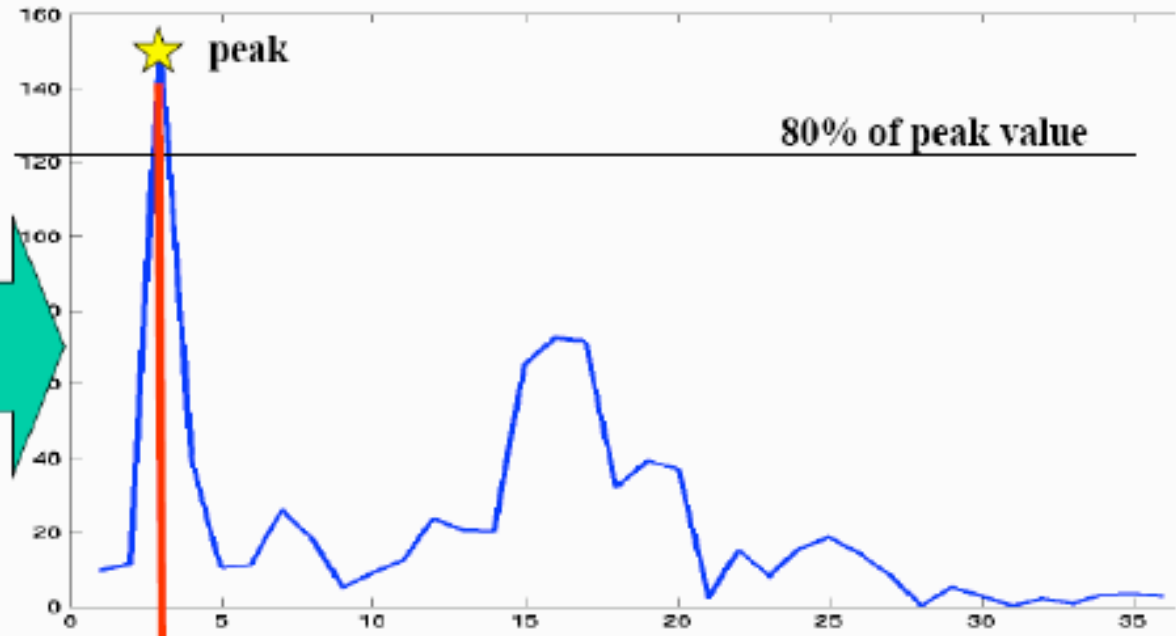
weighted gradient magnitude



gradient orientation



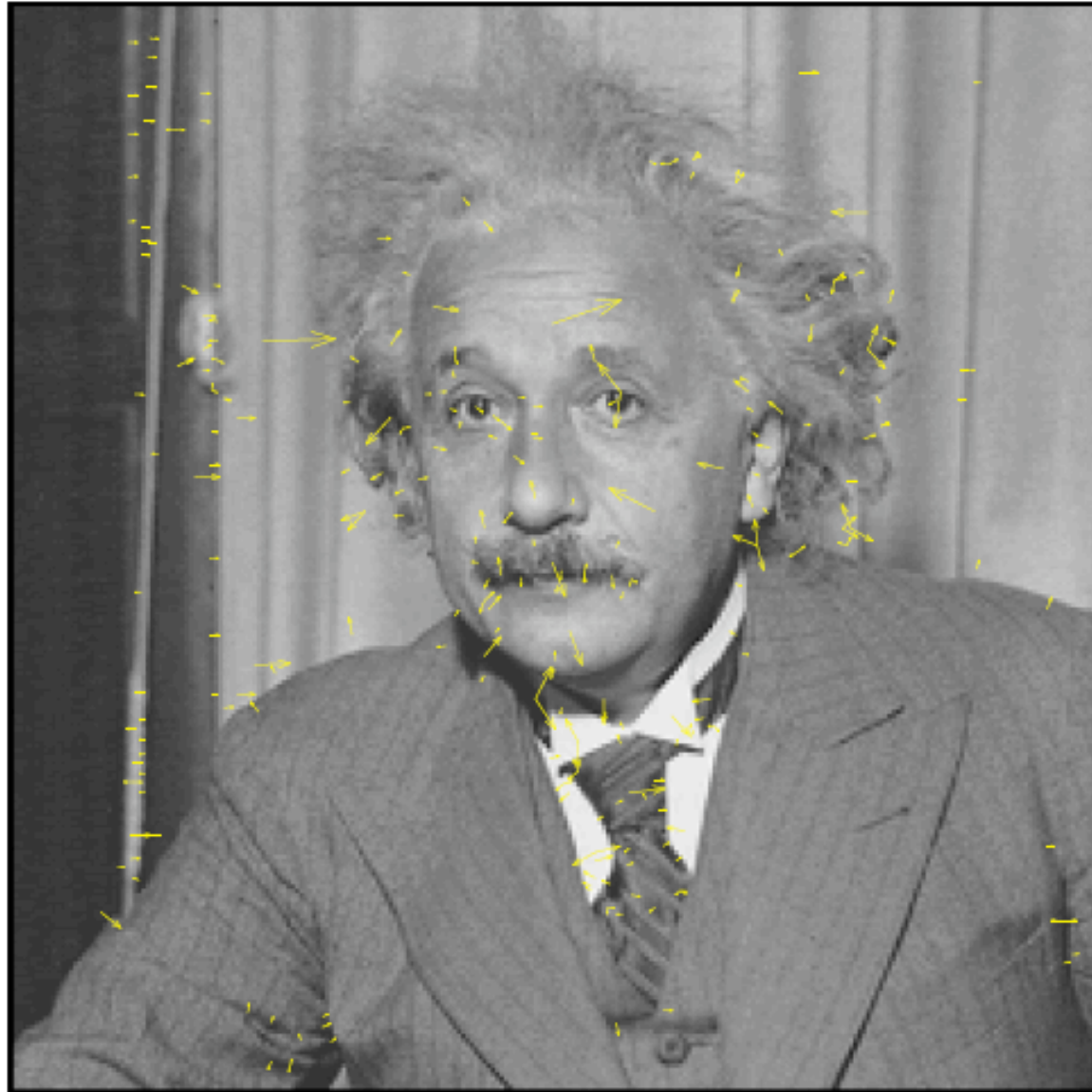
weighted orientation histogram.



20-30 degrees

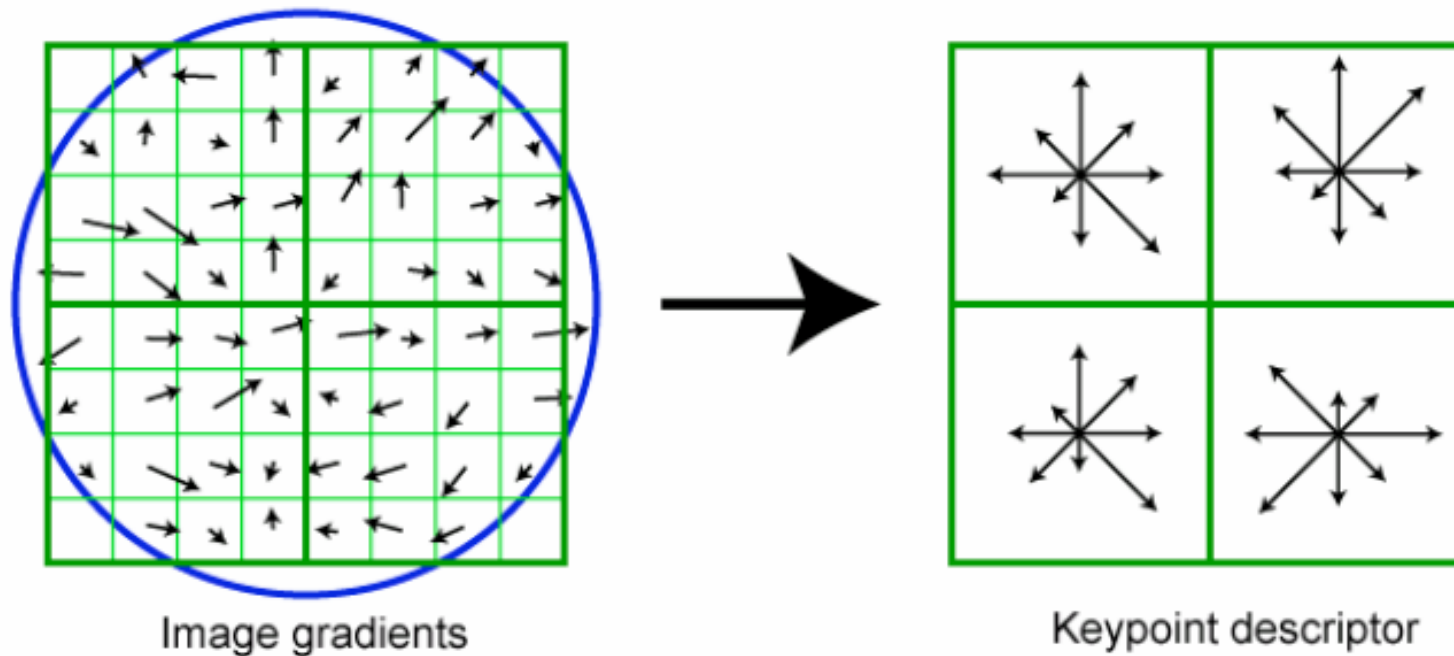
Orientation of keypoint is approximately 25 degrees

SIFT: 3) Orientation Assignment



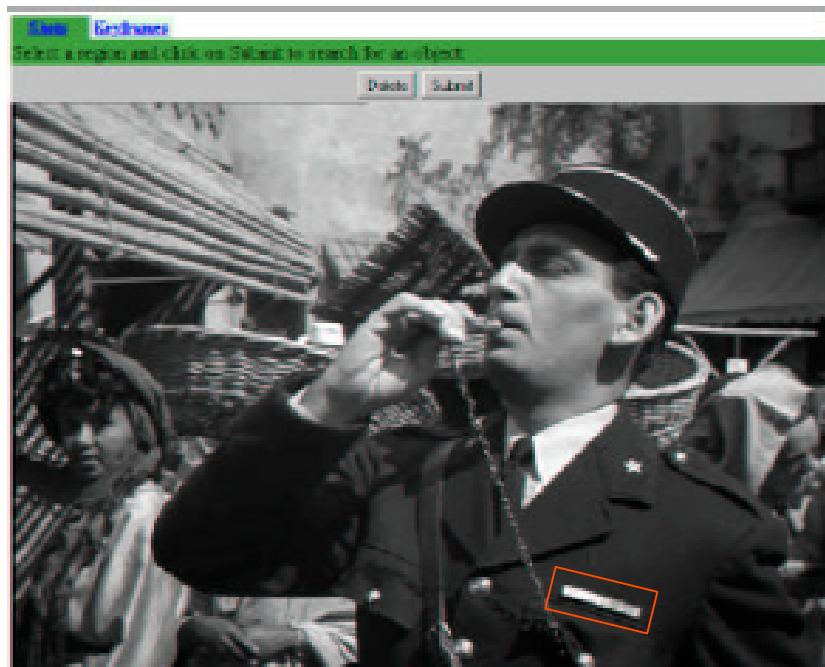
SIFT: 4) Keypoint Descriptor

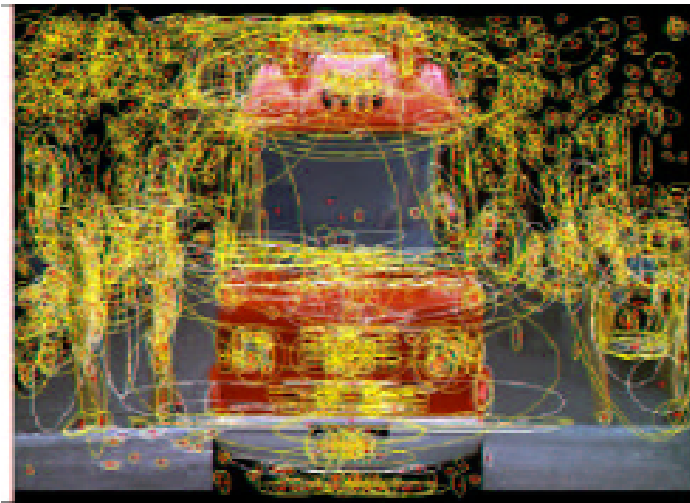
- Thresholded image gradients are sampled over 16x16 array of locations in scale space
- Create array of weighted orientation histograms



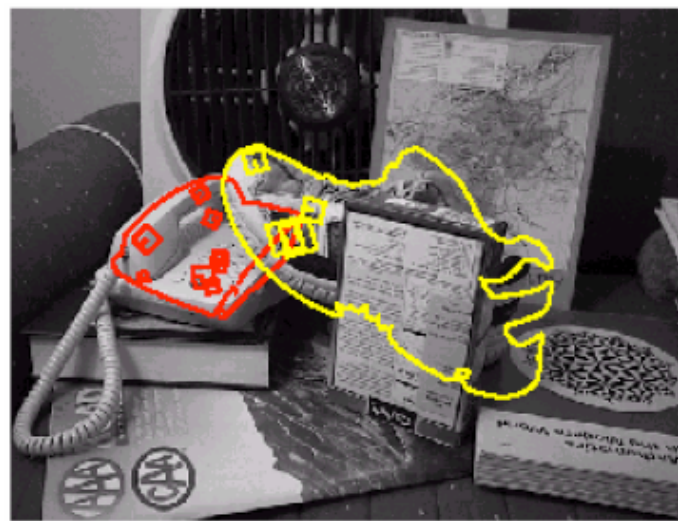
- 8 orientations x 4x4 histogram array = 128 dimensions

SIFT: Application





SIFT: Application



SIFT: Application



- ❑ Invariances:
 - Scaling Yes
 - Rotation Yes
 - Illumination Yes
 - Perspective Projection Maybe
- ❑ Provides
 - Good localization Yes

- **Difficulties of Feature Extraction**
 - ◆ Segmentation
 - ◆ Recognition in Images
 - ◆ Recognition in Document Images
- **Feature Extraction/Detection on the whole Signal**
 - ◆ Global Descriptor
 - ◆ Local Descriptor
- **Feature Extraction/Detection on Objects**
 - ◆ Object Localization / Extraction
 - ◆ Object Characterization
- **Interest of Multi-Resolution**
- **Using Features**

■ Features on Objects

◆ Need to detect Objects in Images

- ◆ Segmentation
- ◆ Difficult task
- ◆ Recognize => Segment but Segment => Recognize
- ◆ See section Segmentation difficulties

◆ Object characterization

- ◆ Features extracted on Segmented Objects

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- Difficulties of Feature Extraction
- Feature Extraction/Detection on the whole Signal
- Feature Extraction/Detection on Objects
 - ◆ Object Localization / Extraction
 - ◆ Region Labeling
 - ◆ Edge Detection
 - ◆ Connected Components Labeling
 - ◆ Skeletonization
 - ◆ Handwriting extraction
 - ◆ Line-Segment Detection
 - ◆ Object Characterization
- Interest of Multi-Resolution
- Using Features

- **Criteria: Luminosity, Color, Texture...**
 - ◆ **Homogeneous Regions / Criteria**
 - ◆ **Significant Criteria Difference**

- **Simple Inside, no small holes**

- **Regular Edges**

- **Measure Space Partition**

- **Region Growing**
 - ◆ Find a Germ
 - ◆ Aggregation

- **Edge-Region Duality**
 - ◆ Edge Detection
 - ✦ See next section
 - ◆ Fill inside

- **Using Time in Image Sequence**
 - ◆ Object Movement can be detected
 - ◆ What Changed from one image to another
 - ◆ Follow Object

■ Measure Space

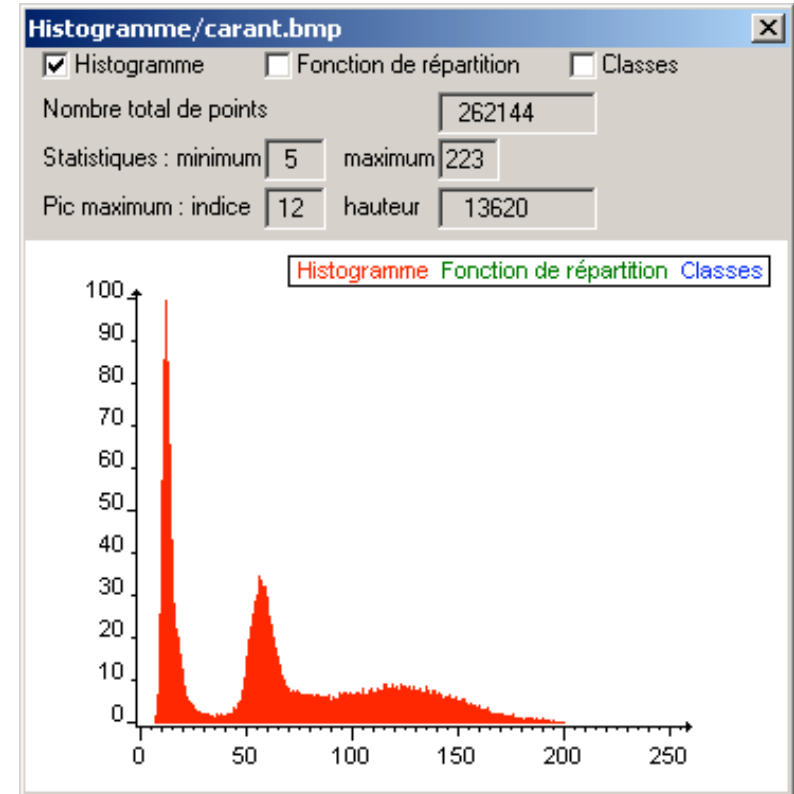
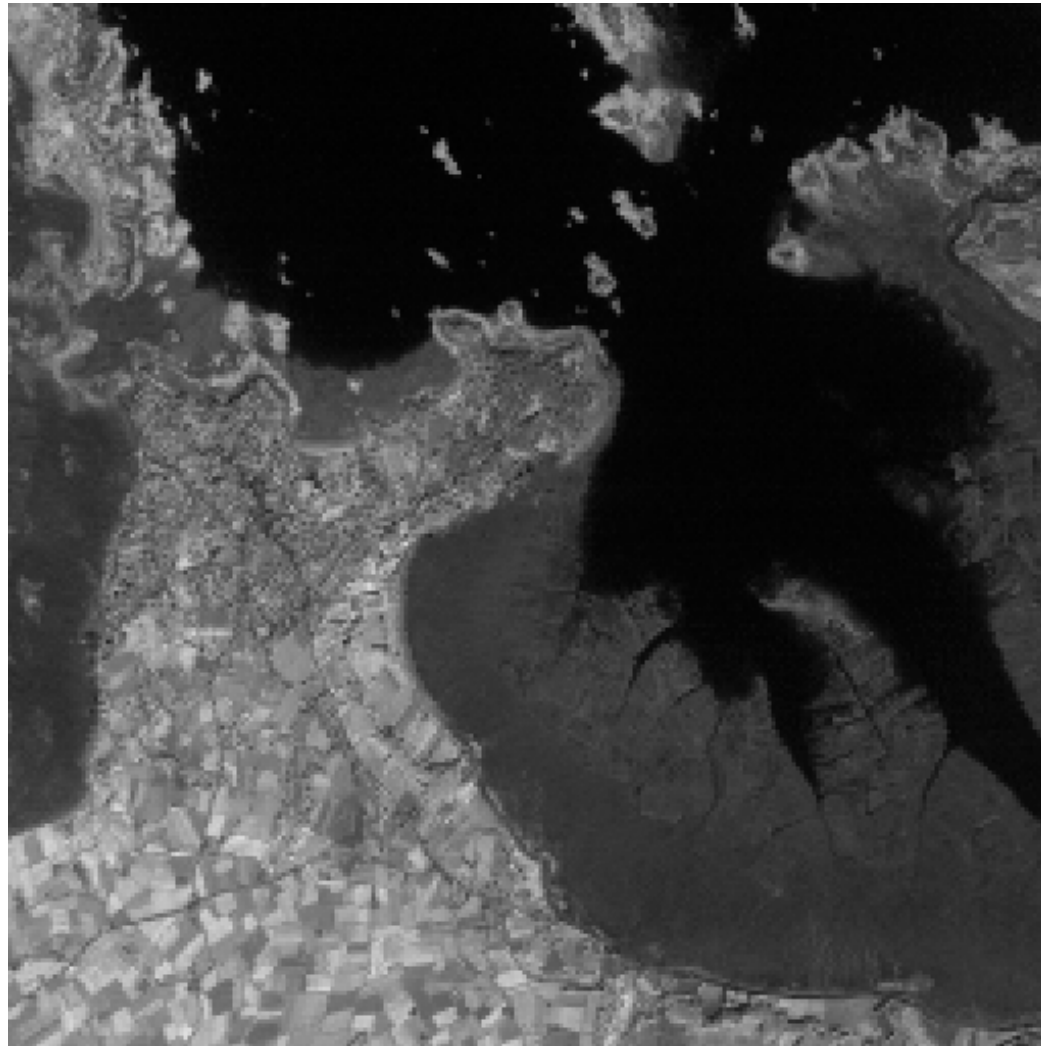
- ◆ Luminosity
- ◆ Color
- ◆ Texture
- ◆ Gradient

■ Measure Space Partition

- ◆ For example: black/white

■ Pixel Labeling by a class name

- ◆ Connected Components of the same name

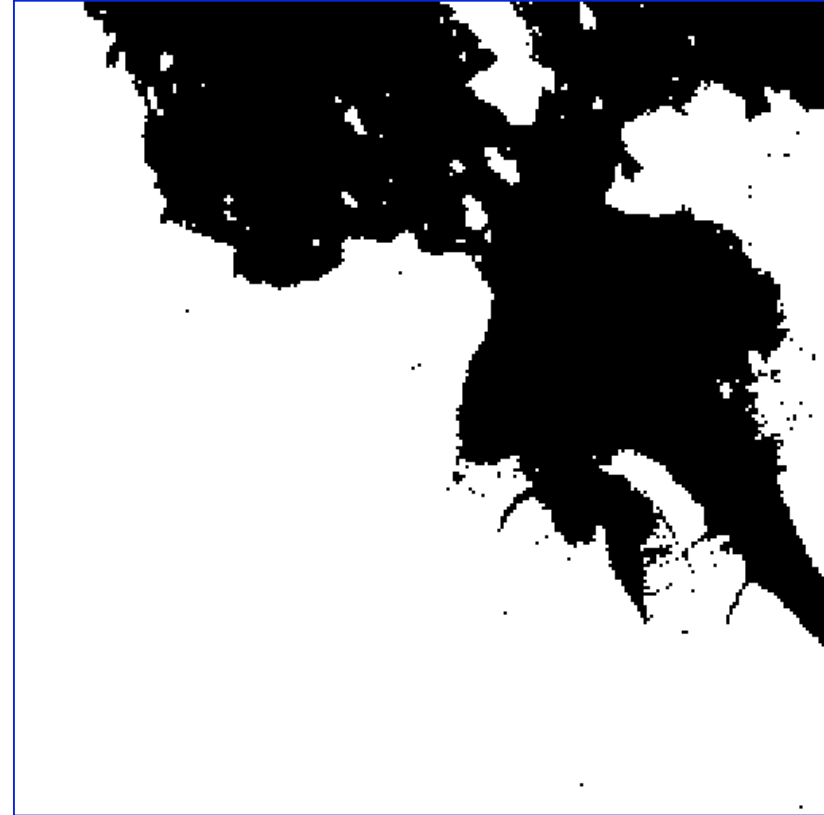
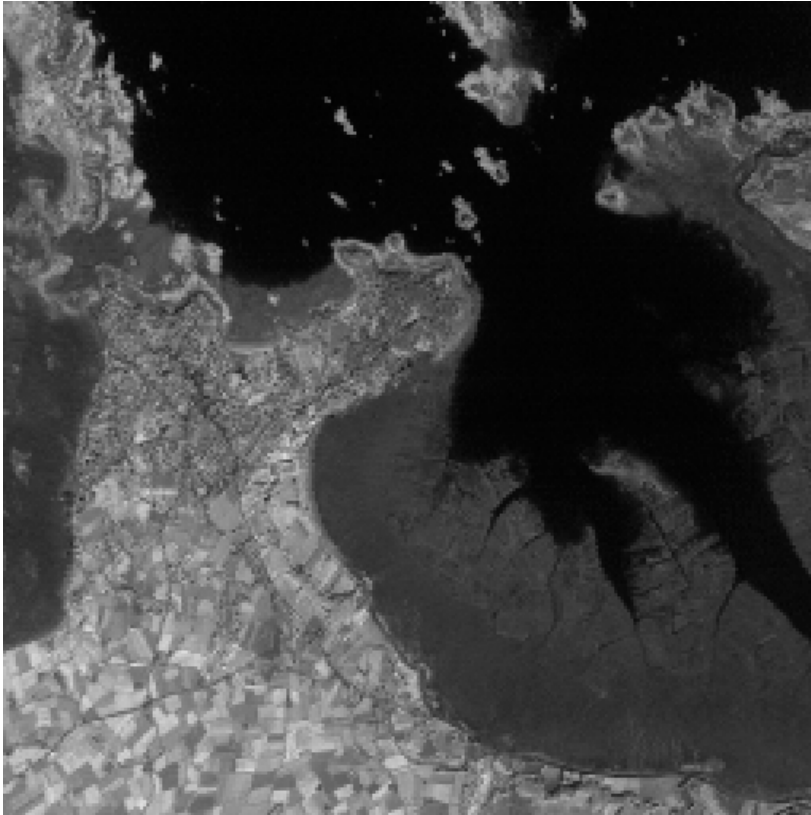


Seuil manuel

0-40 eau

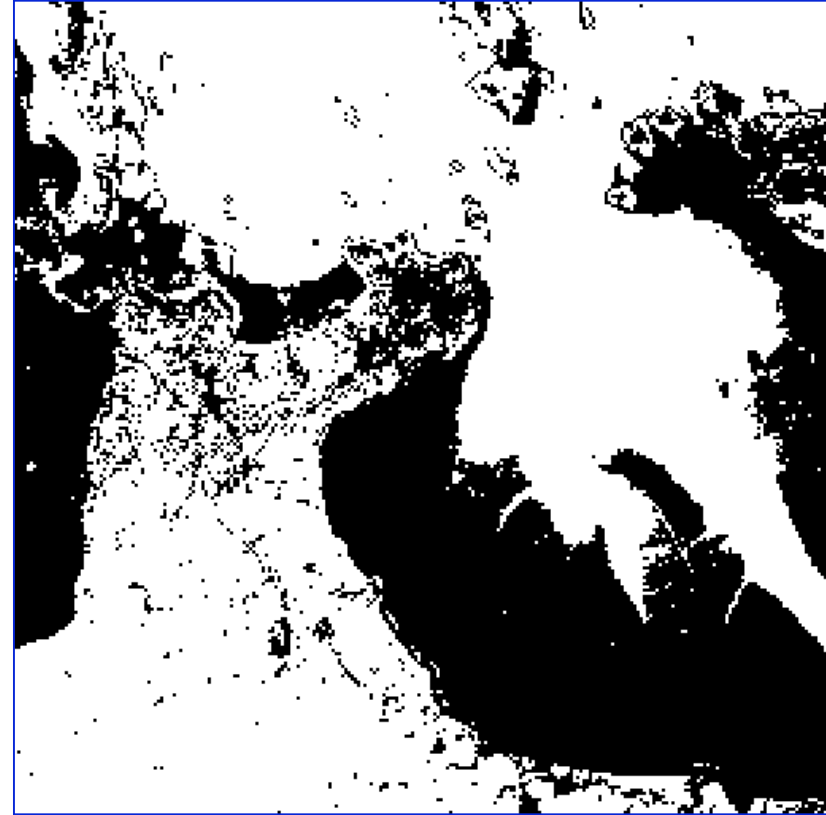
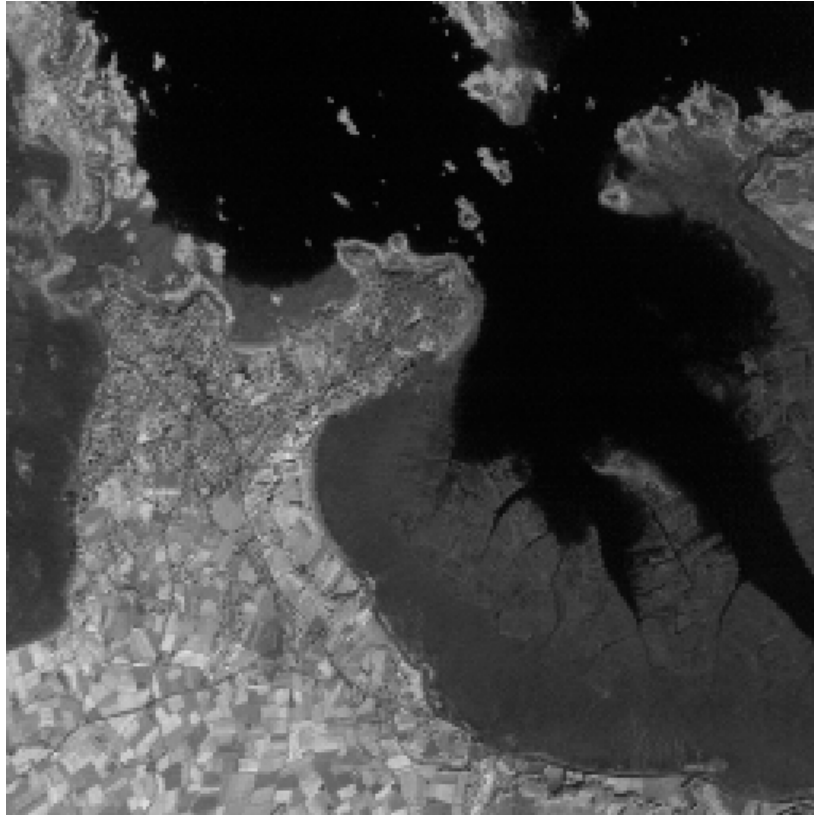
41-98 estran

>98 terre



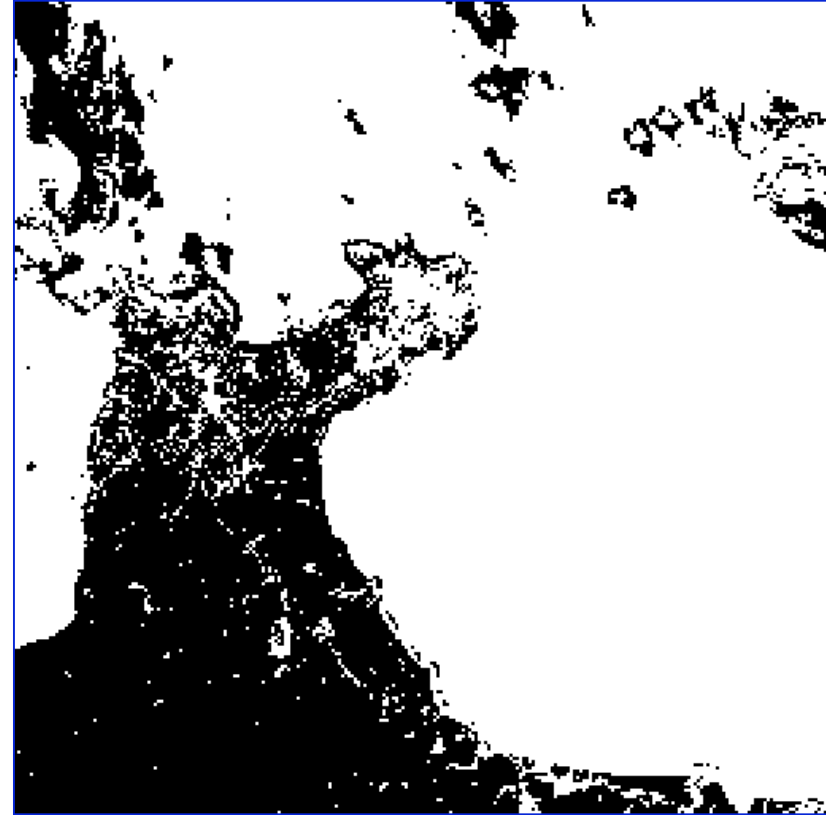
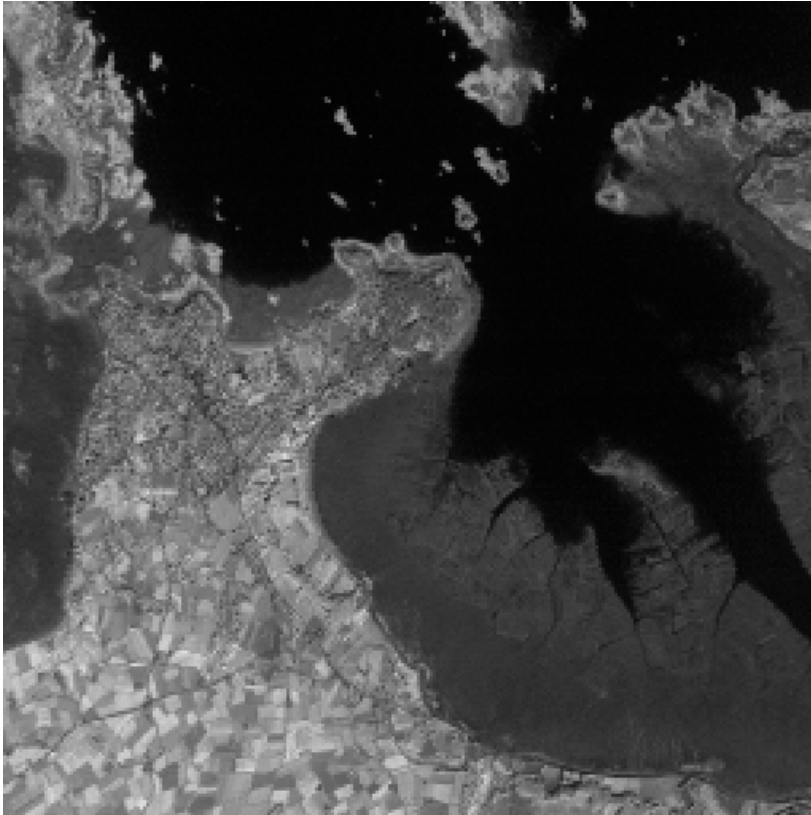
eau < 40

Noter les pixels isolés



$41 < \text{estran} < 98$

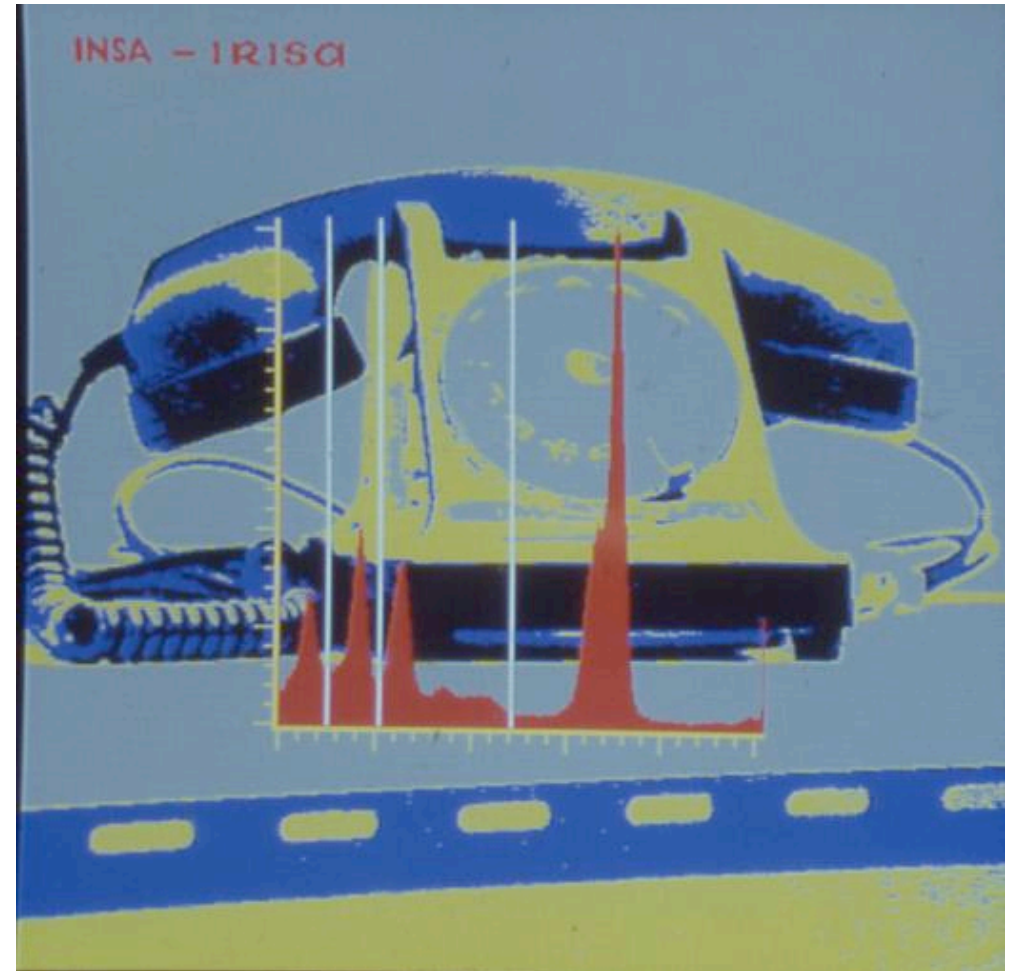
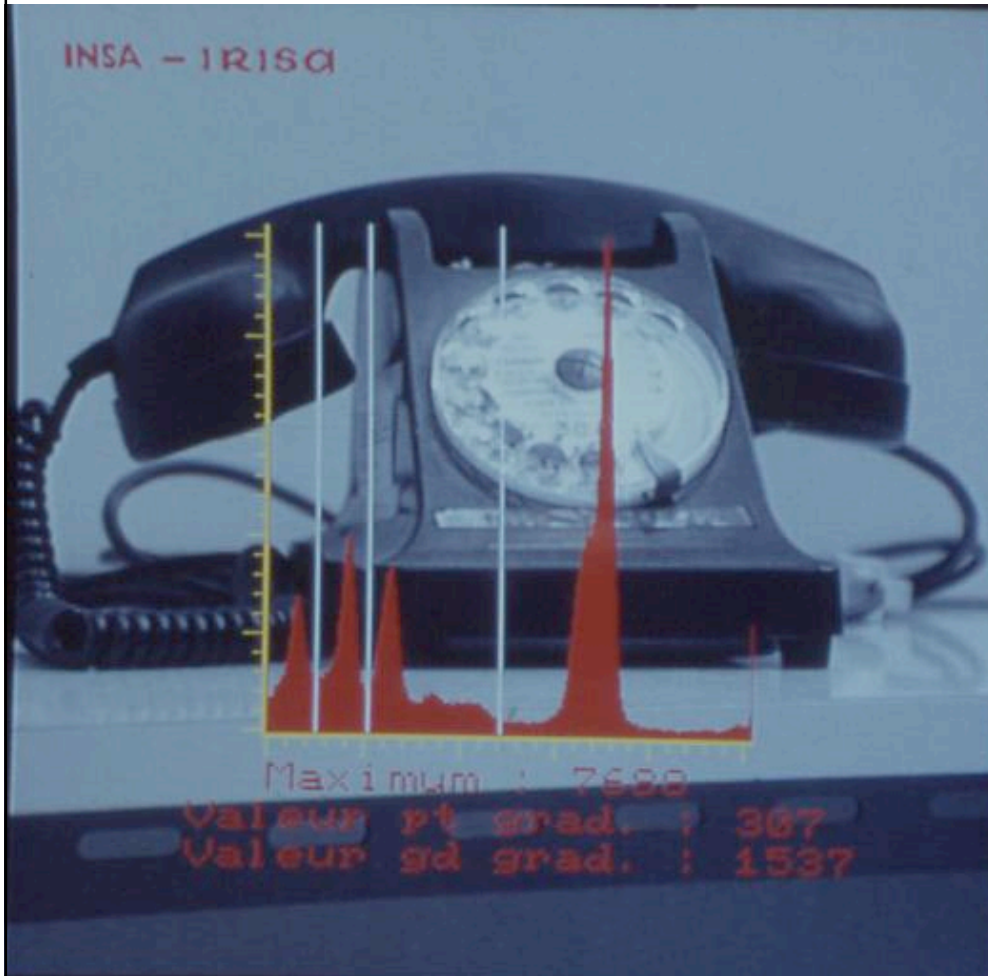
Besoin d'un critère en plus



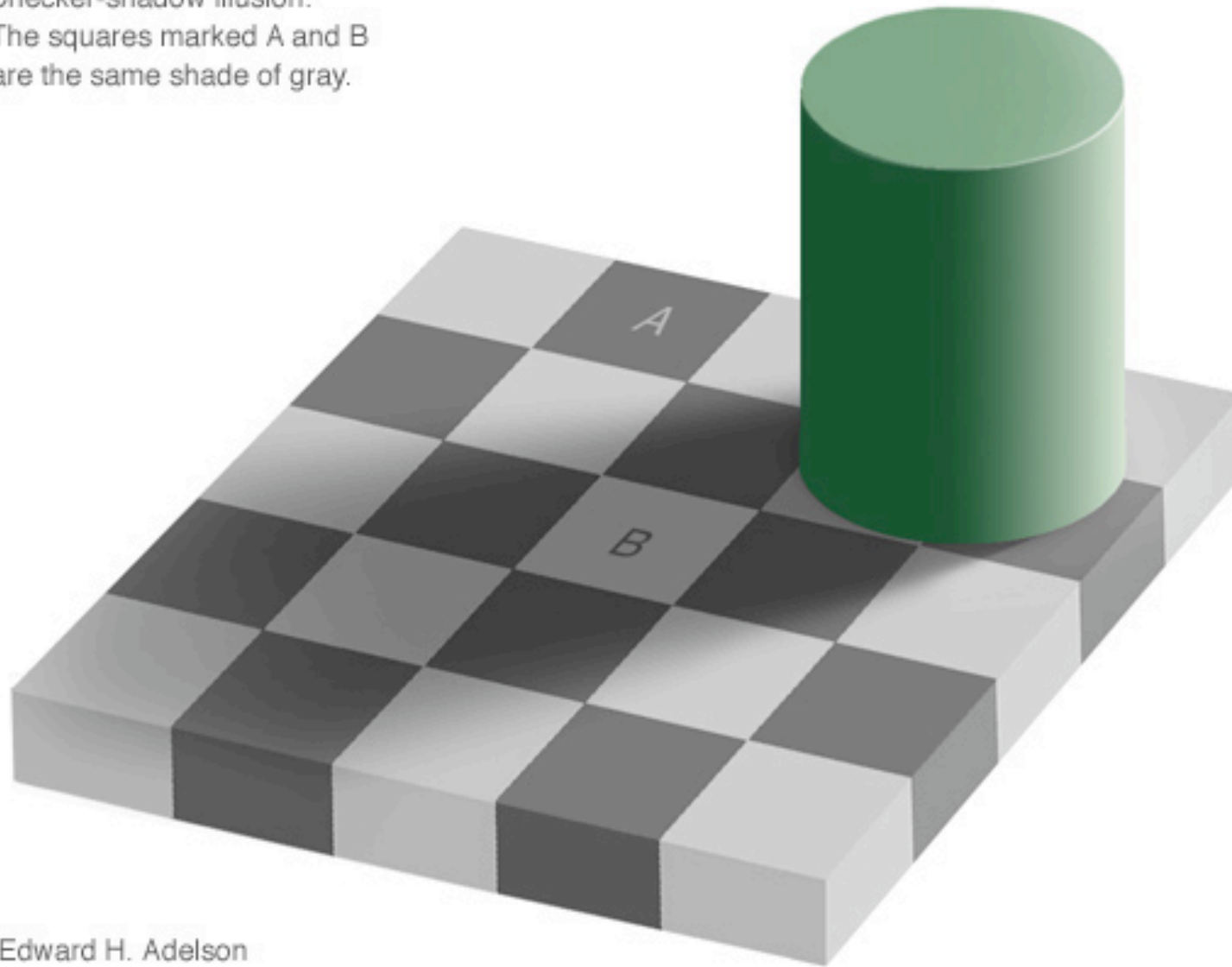
terre > 98

Besoin d'un critère en plus

Multi-Class Luminosity Partition

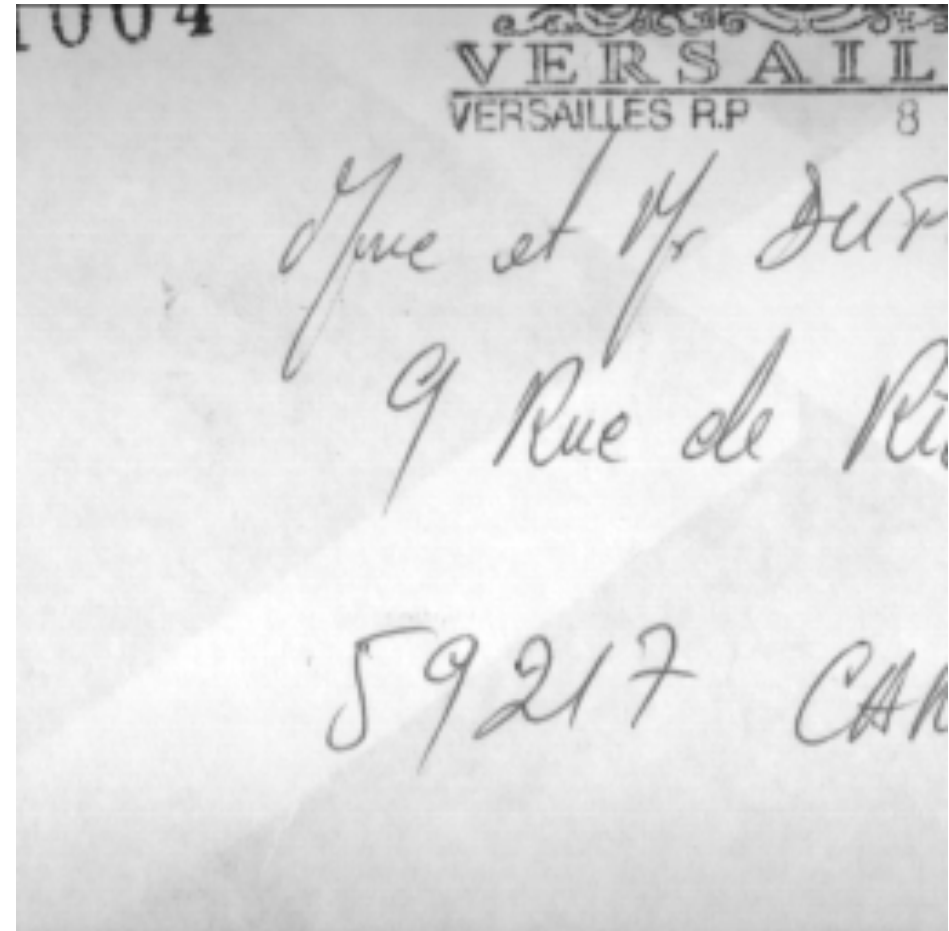
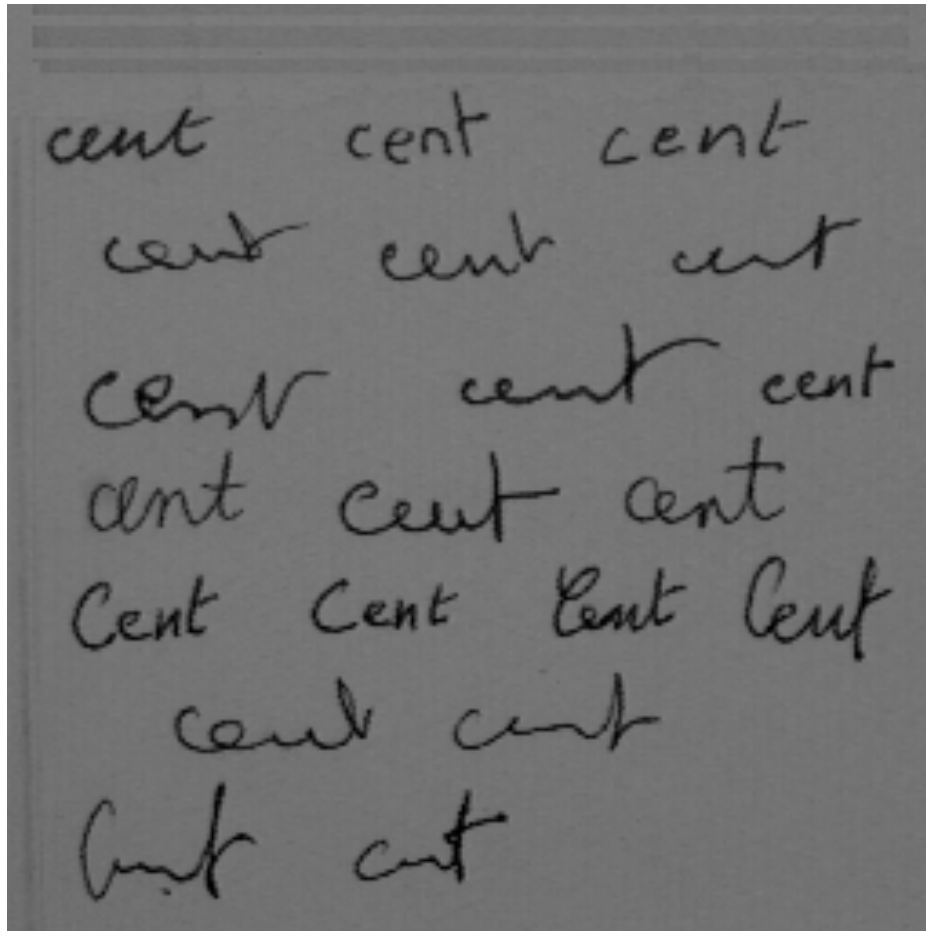


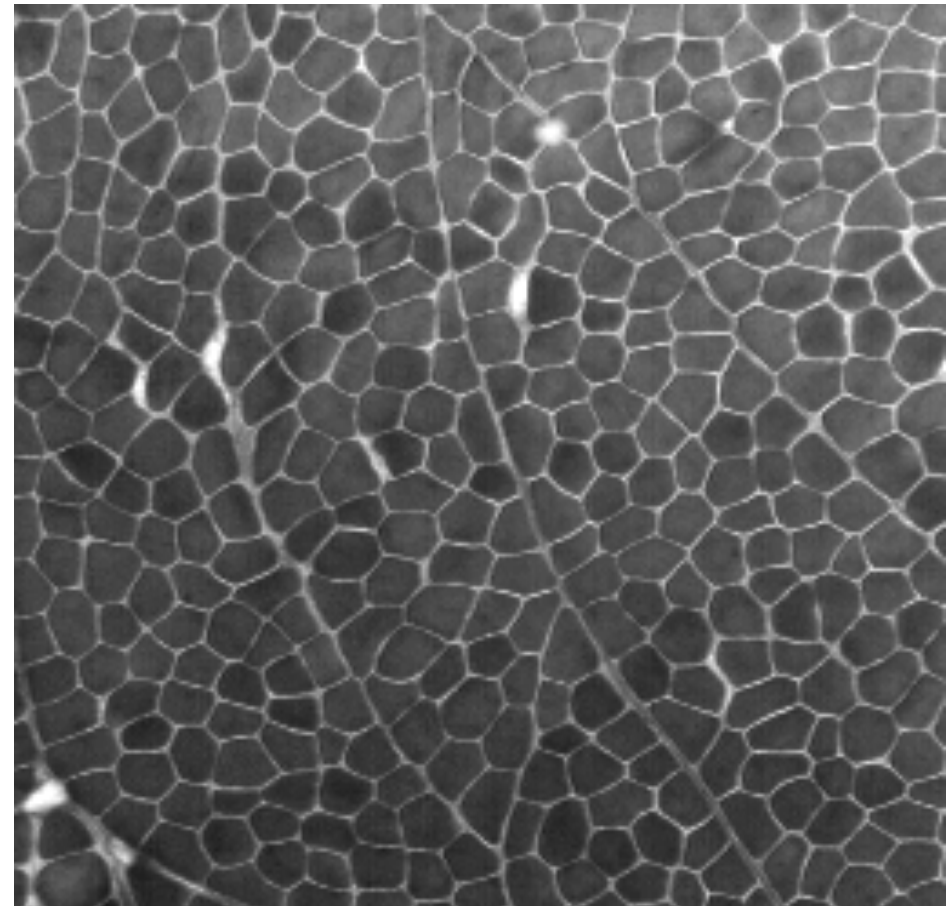
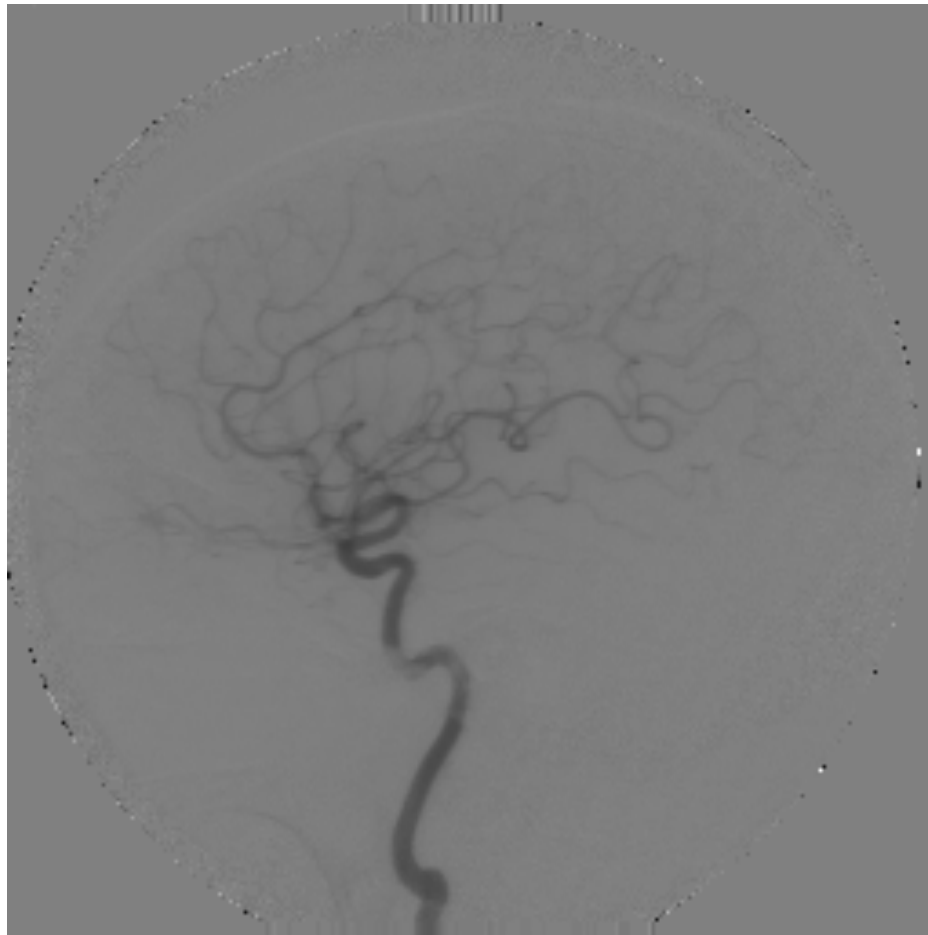
Checker-shadow illusion:
The squares marked A and B
are the same shade of gray.



Edward H. Adelson

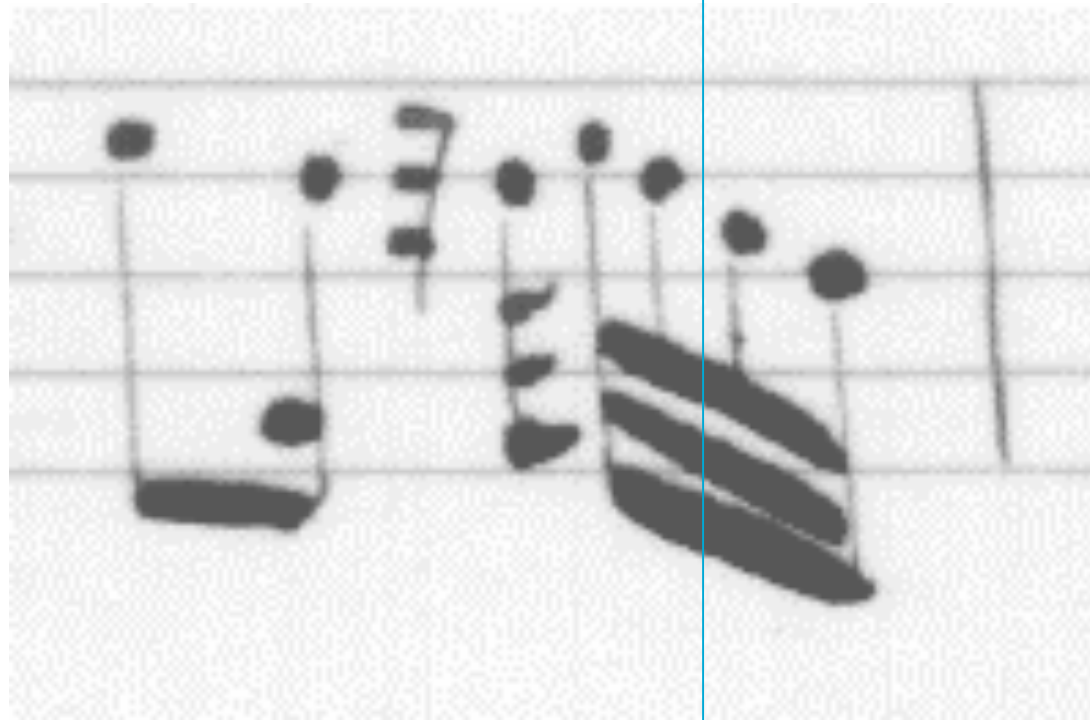
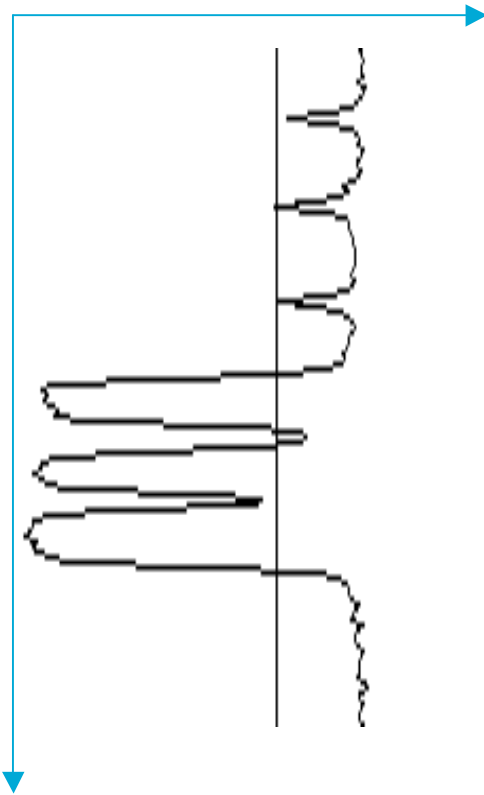
Binarization Possible on Text Images

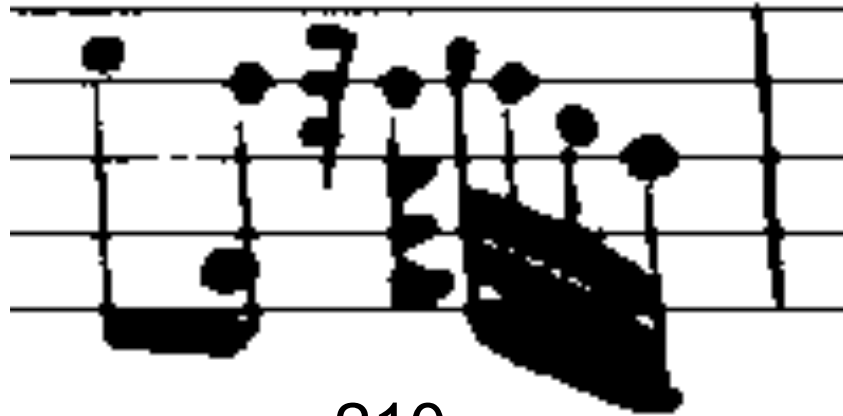






Luminosité





210



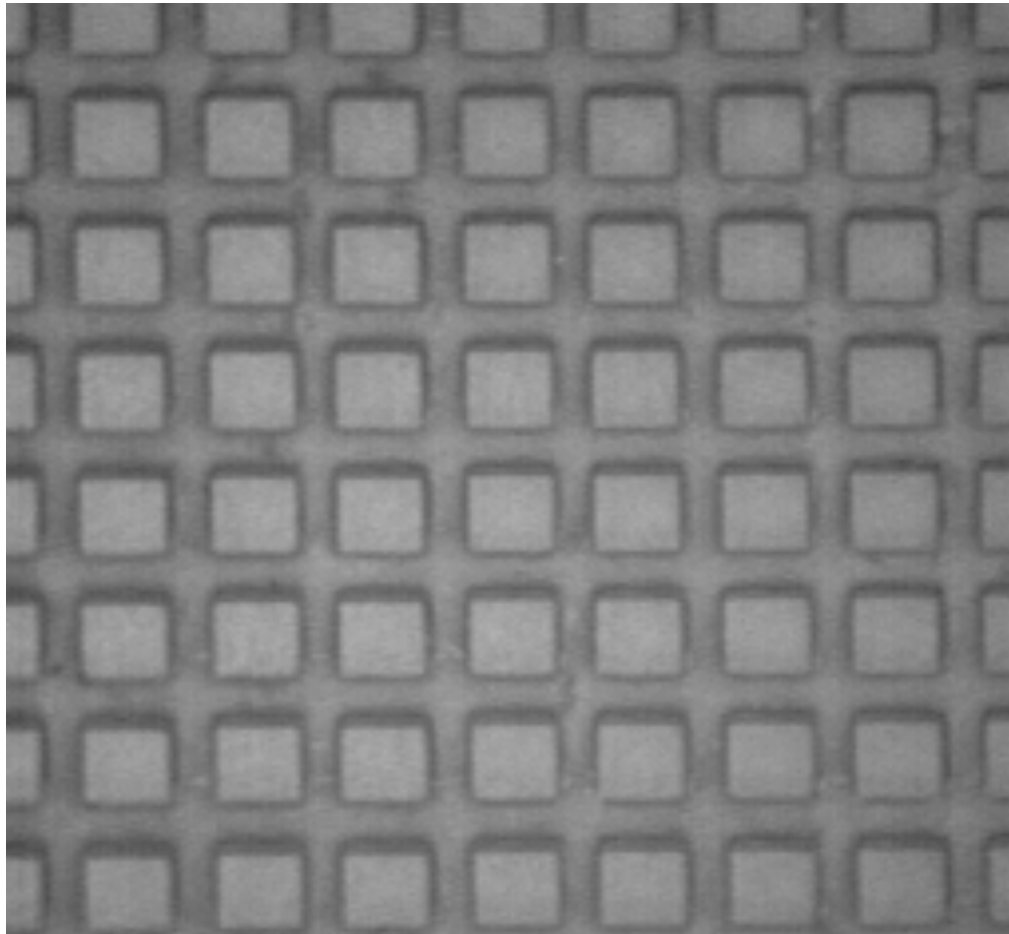
195



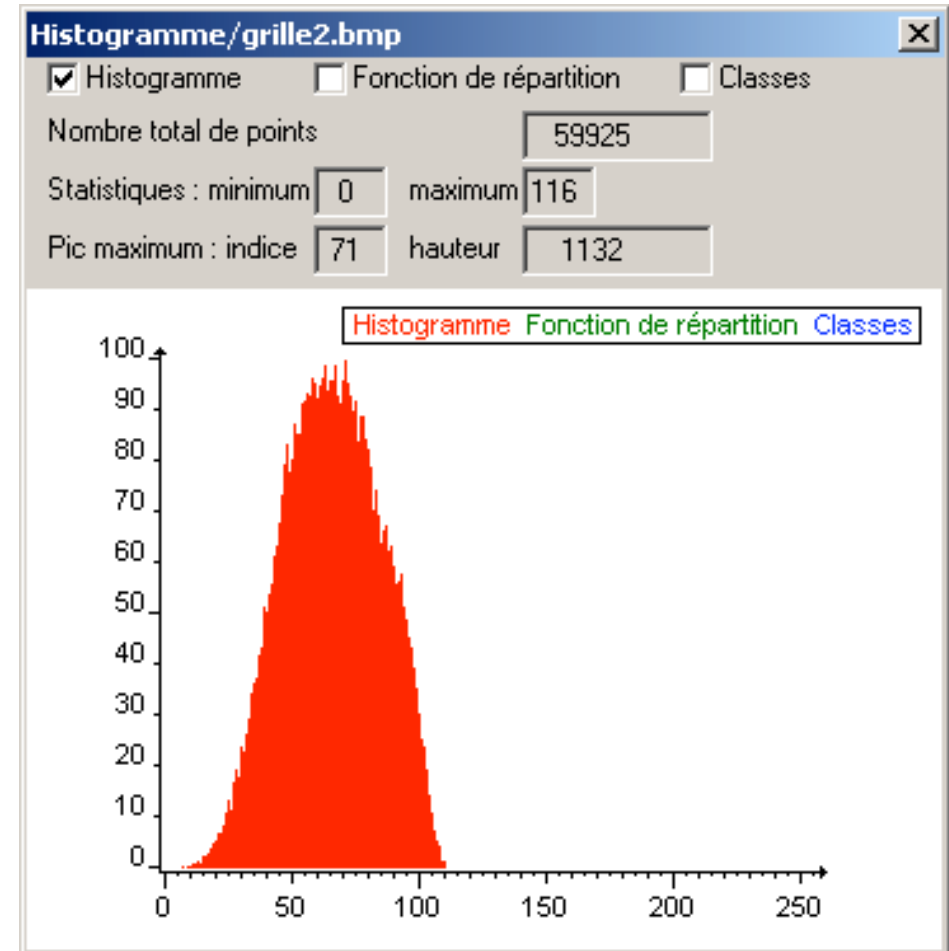
110



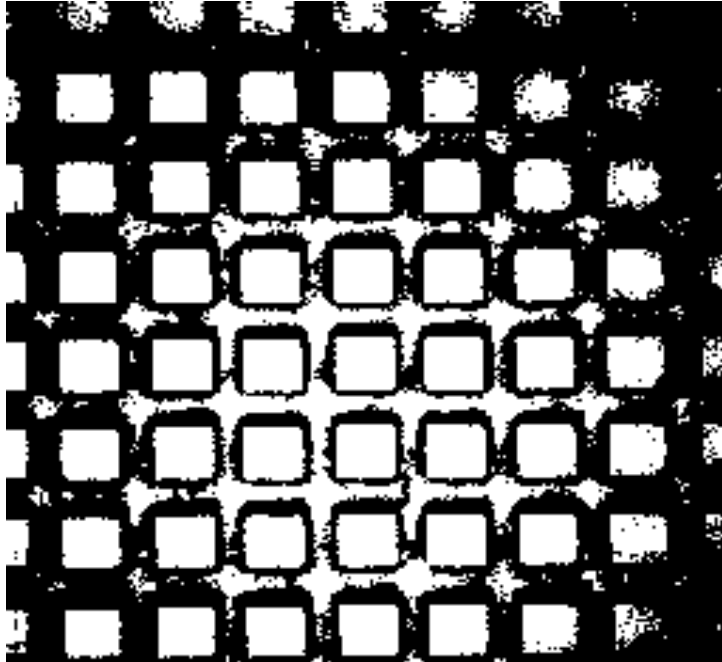
Seuillage adaptatif



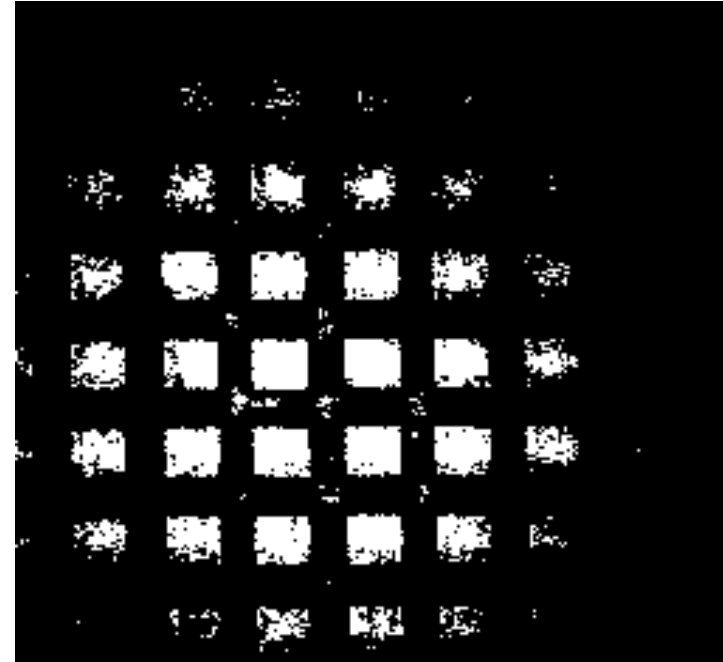
Bi-Modal Image



Mono-Modal Histogram



Threshold at 71, max peak



Too high threshold

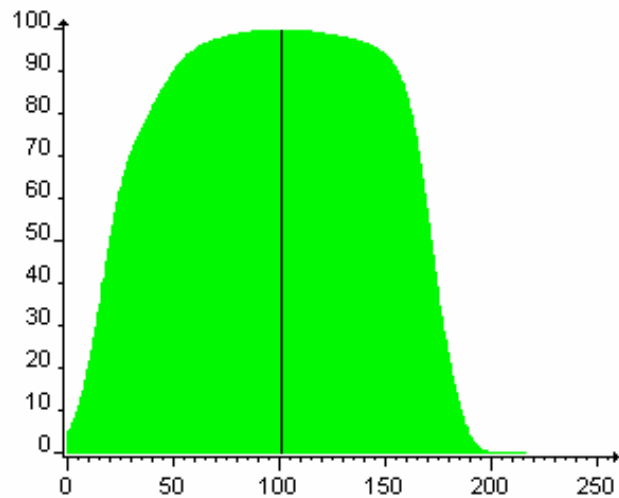
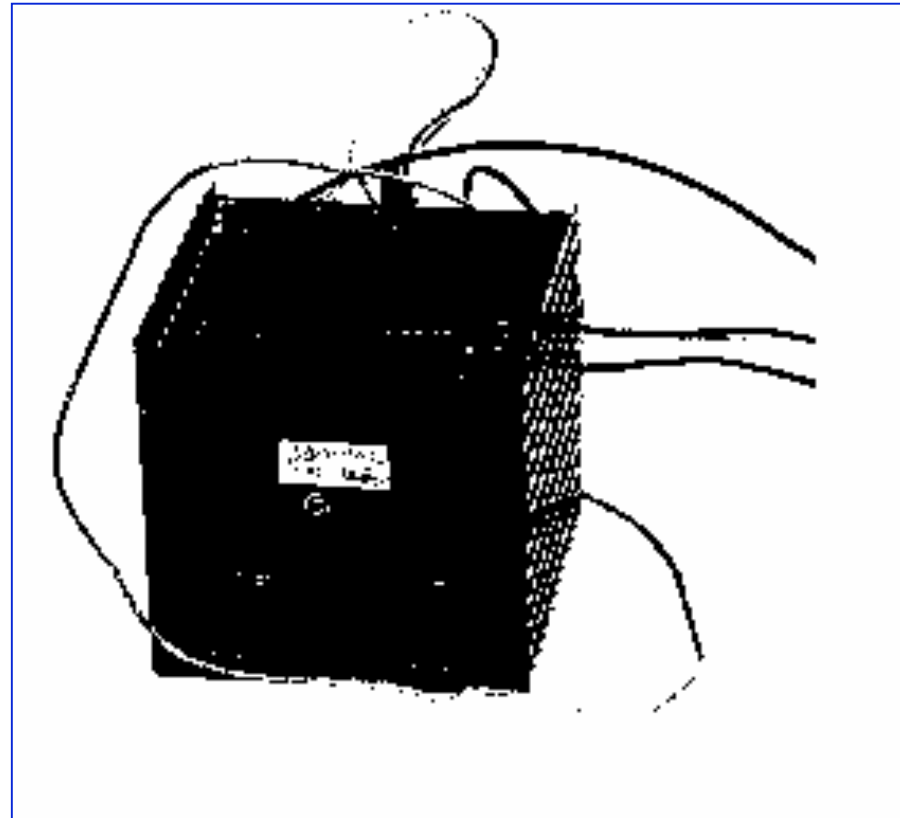
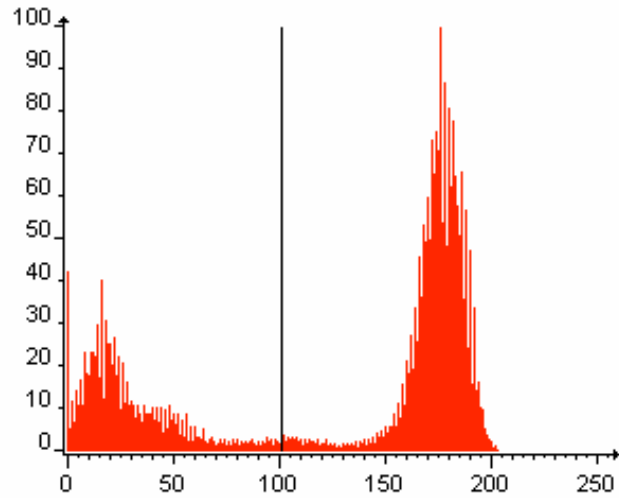
Conclusion: non uniform lightning

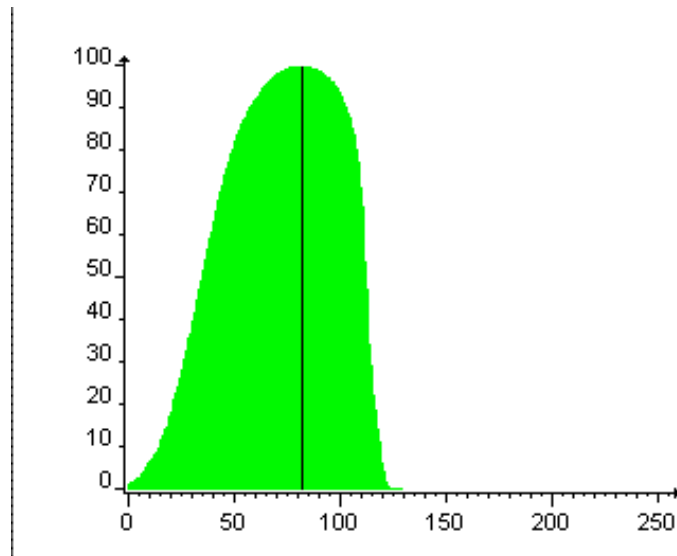
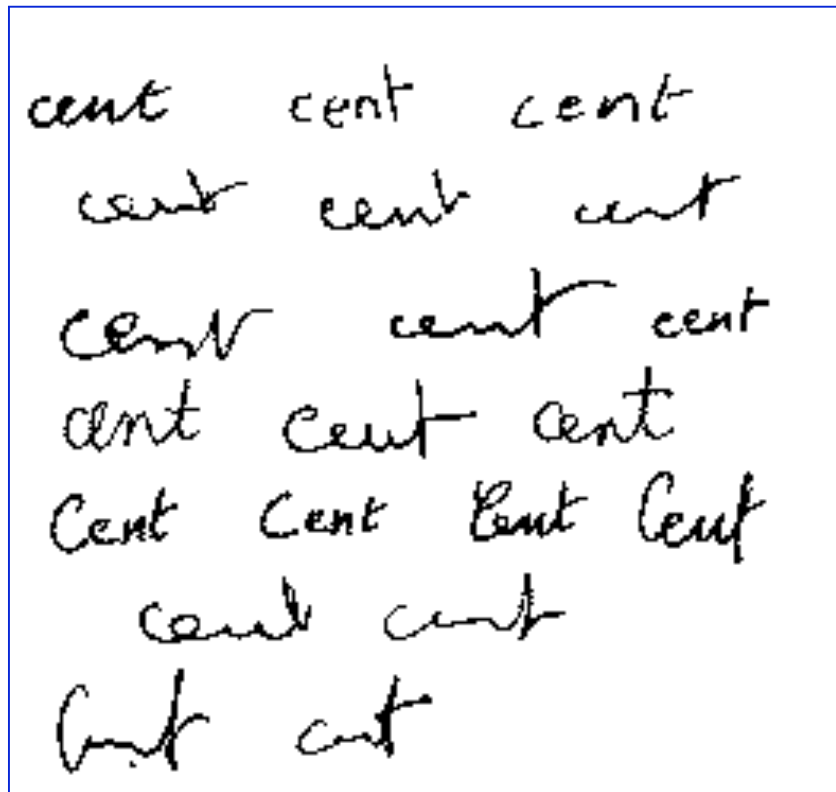
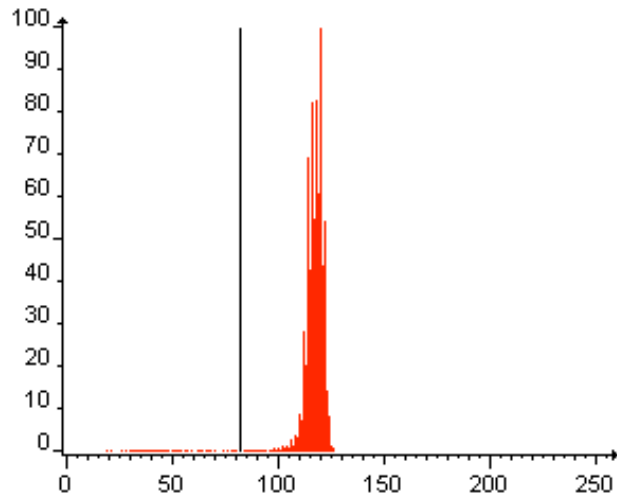
■ Global Methods

- ◆ Interclasse Variance : Otsu
- ◆ Histogram Concavity Analysis
- ◆ Entropy : Pun
- ◆ Moments
- ◆ Histogram Modification: Mason
- ◆ Transition Matrix: Deravi
- ◆ ...

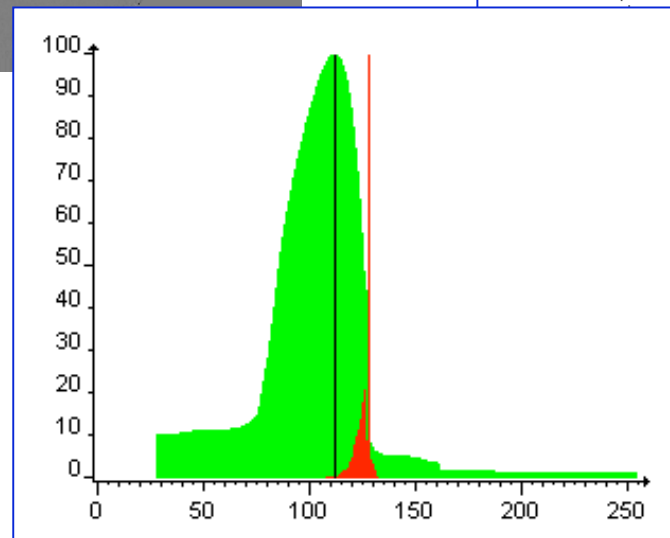
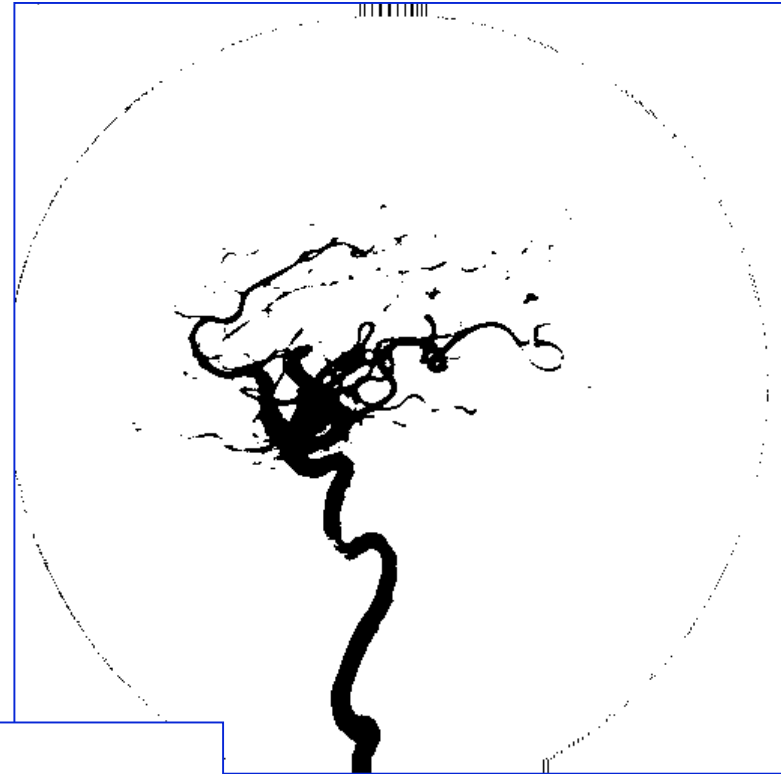
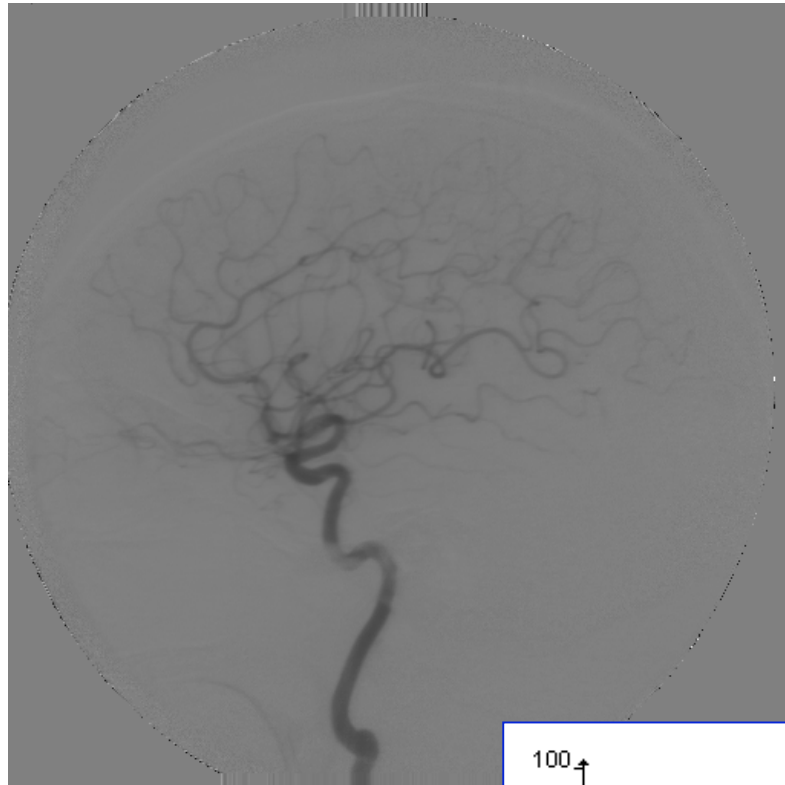
■ Local Methods

Binarization: Otsu Method



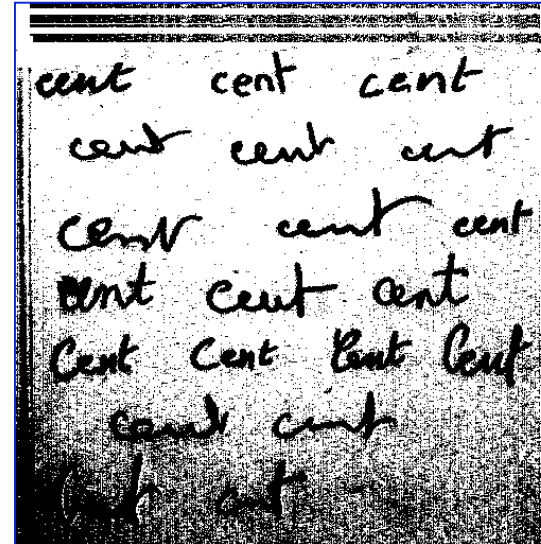
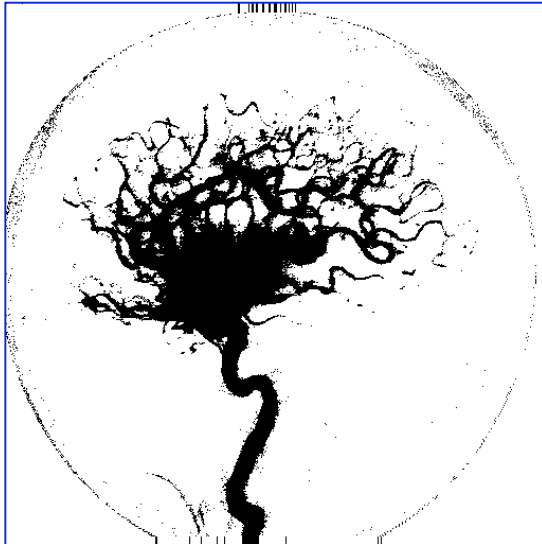


Binarization: Otsu Method



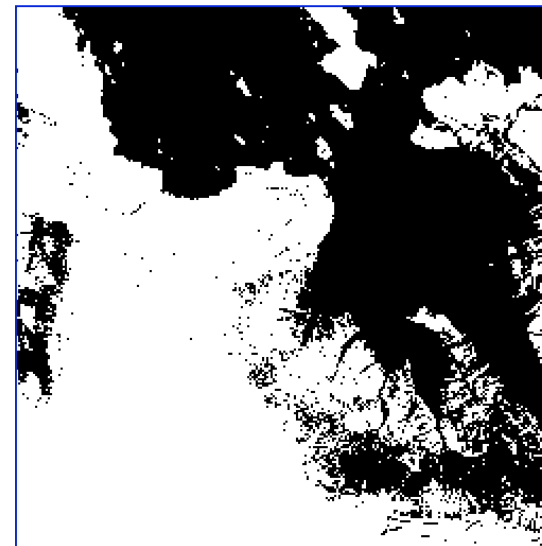
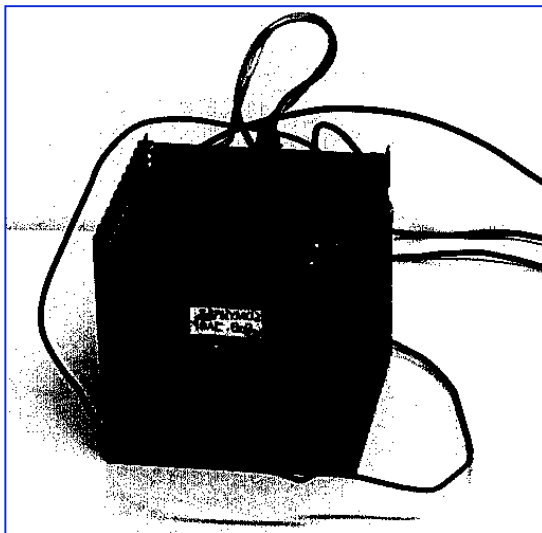
Binarization: PUN Method

121



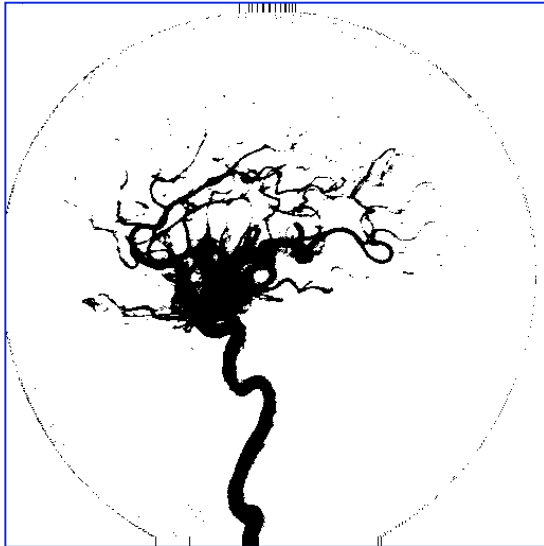
116

157



57

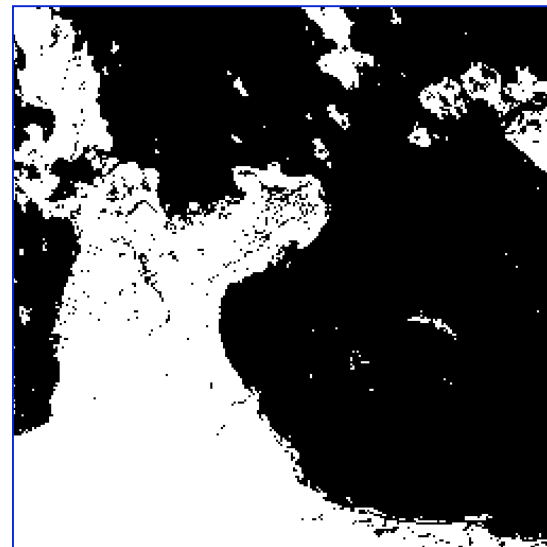
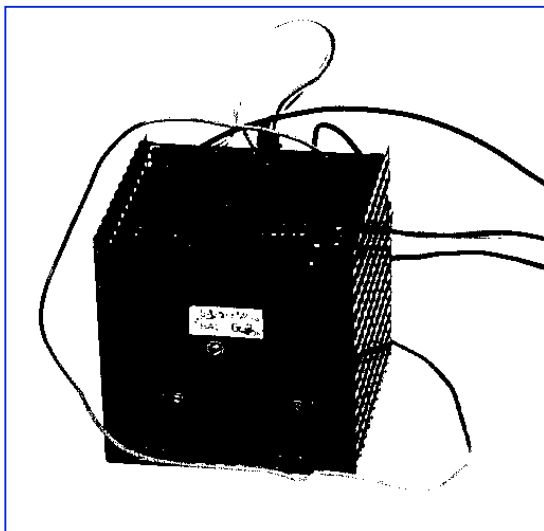
117



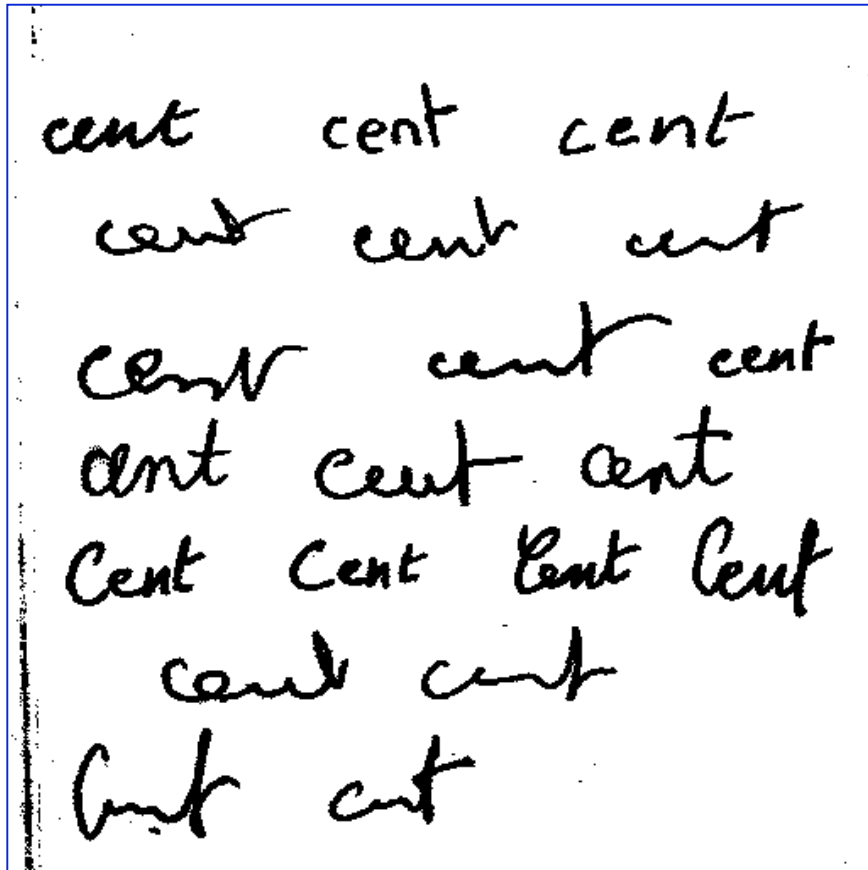
cent cent cent
cent cent cent
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cent cent

85

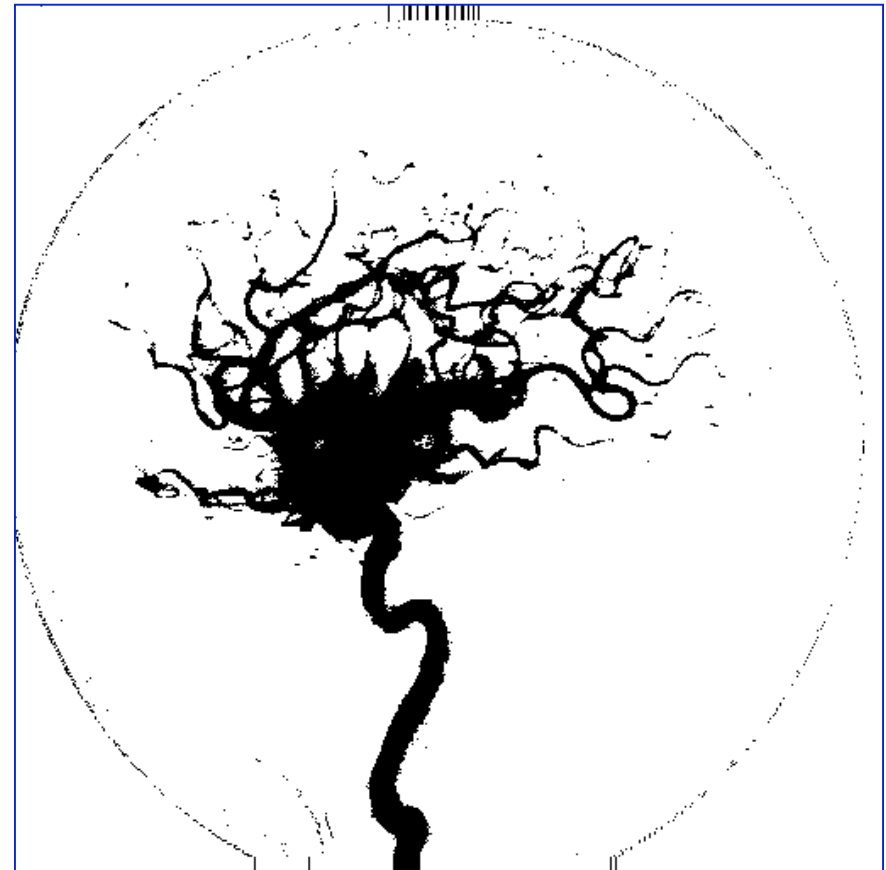
100



77

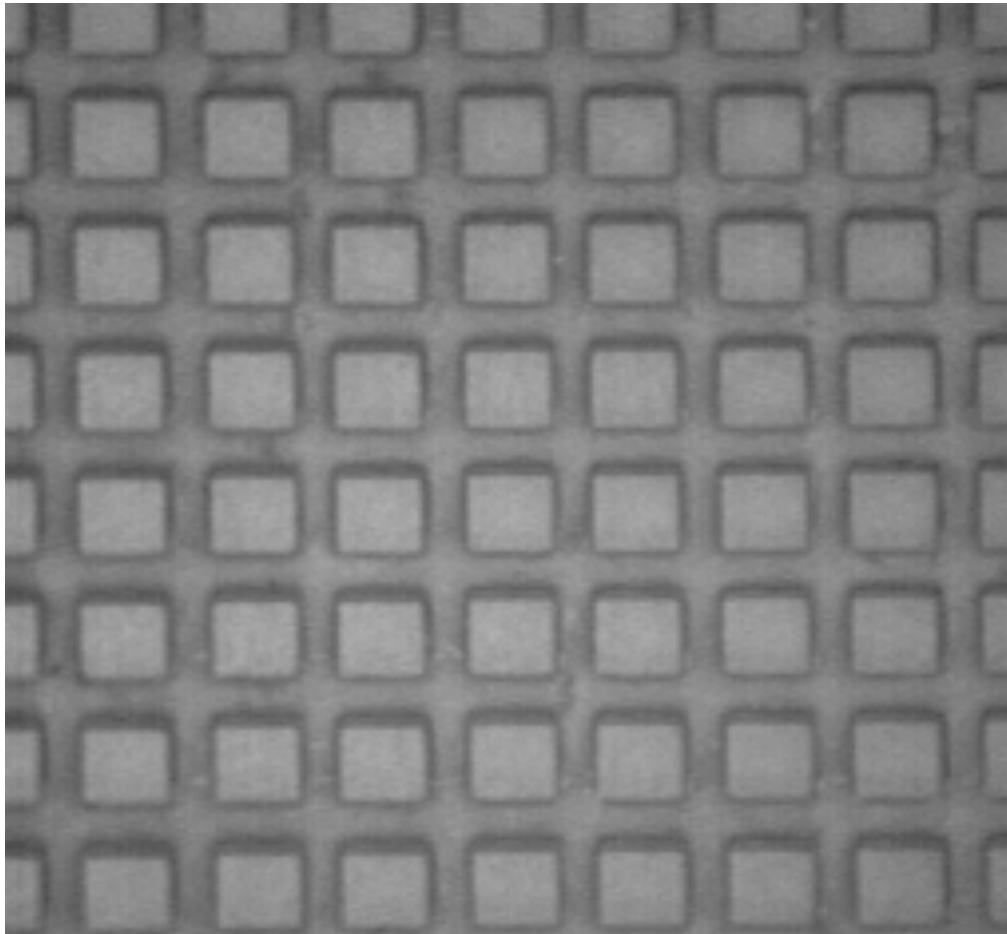


106

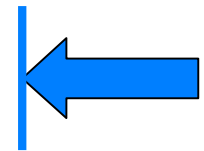
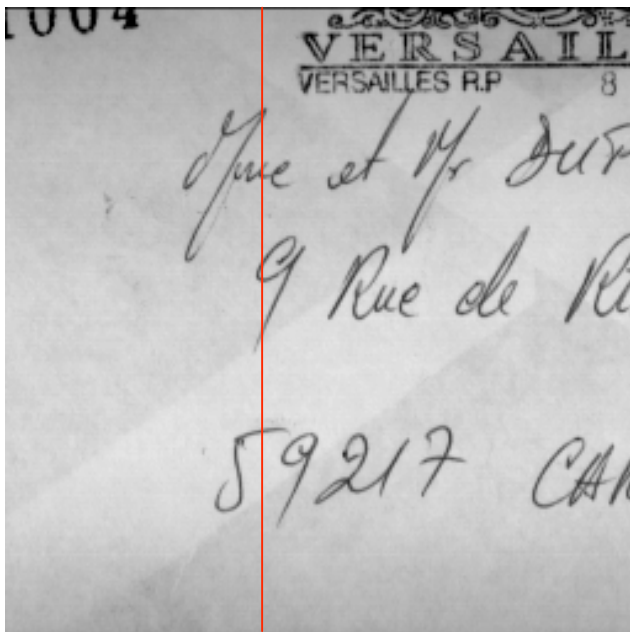
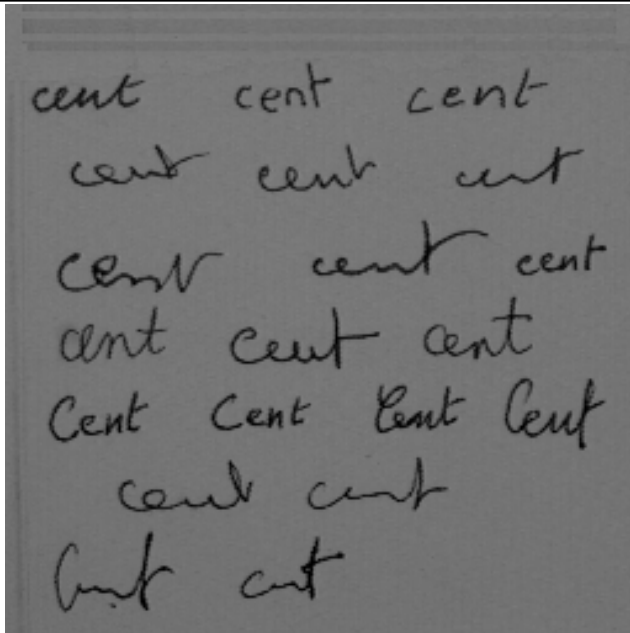


119

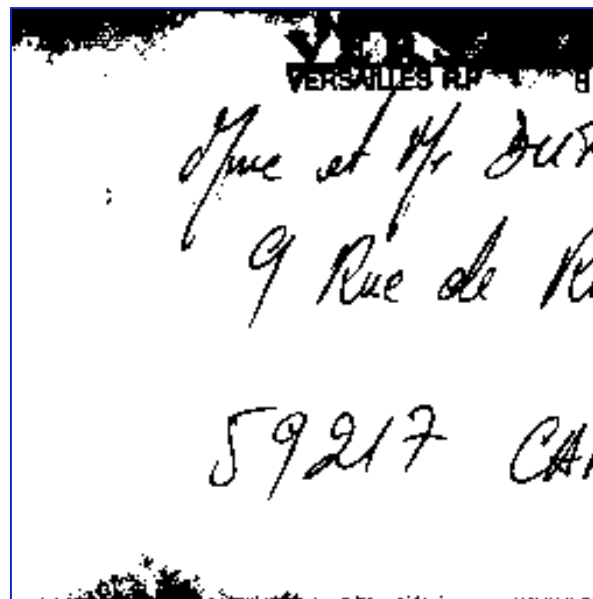
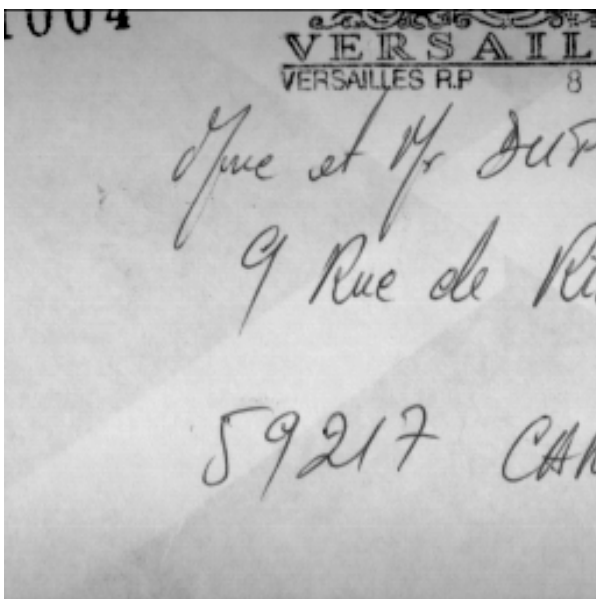
- Lot of Different Methods
- None really usable
- Problem
 - ◆ Global Threshold



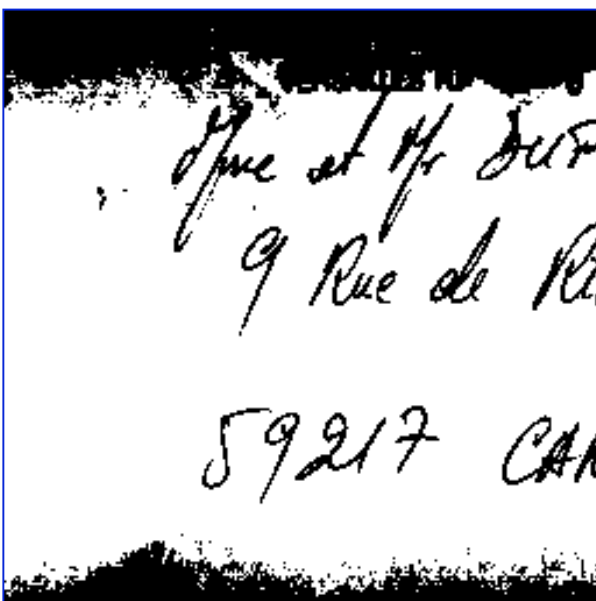
Non-uniform Lightning: Column



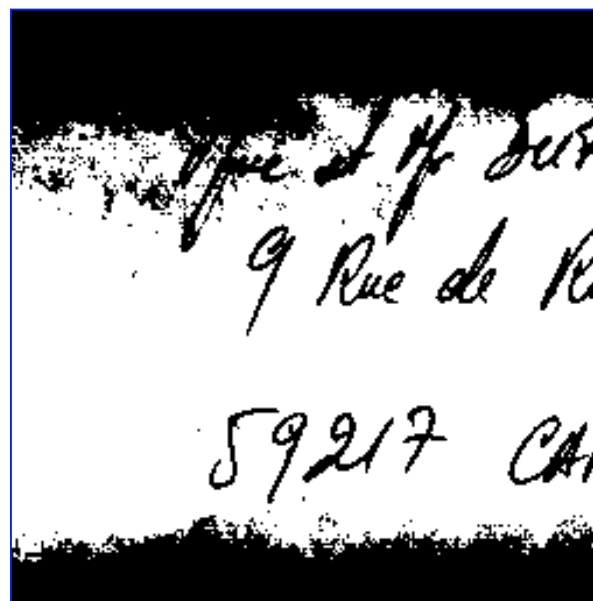
Non-uniform Lightning: Column



170



180

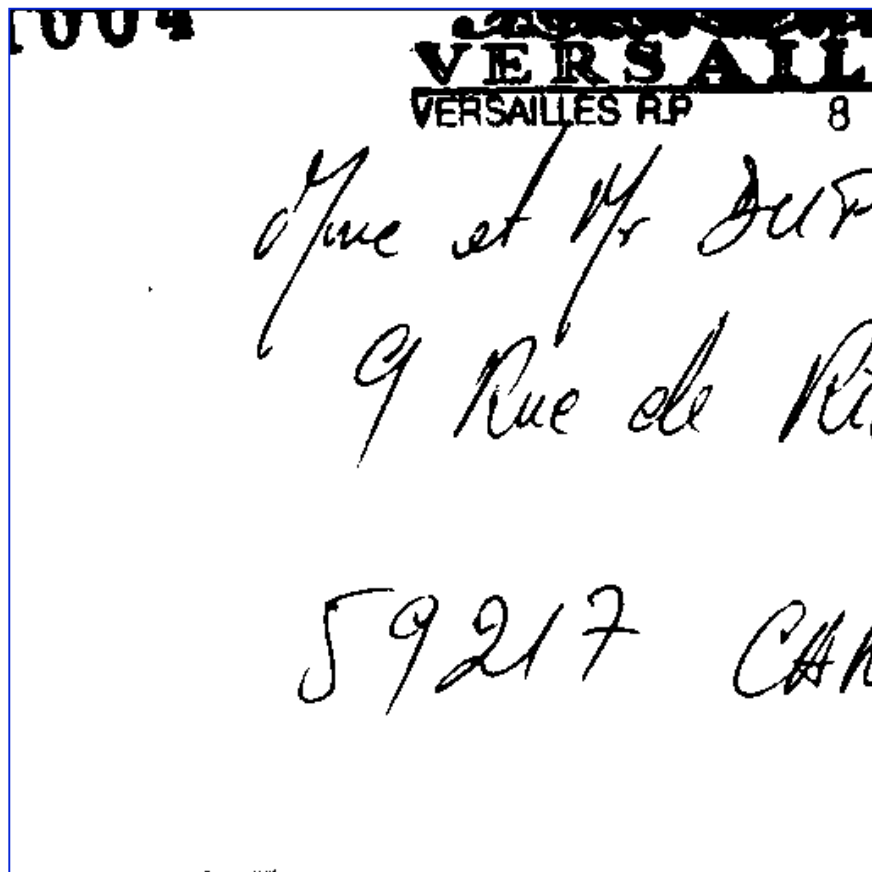


190

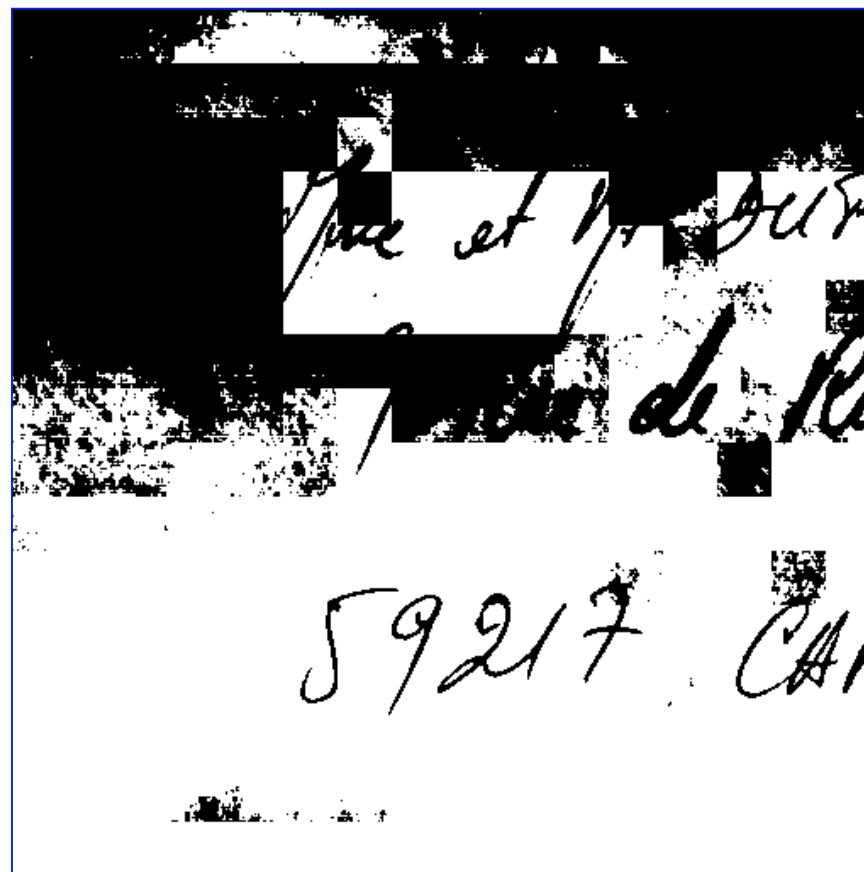
- **Split Image in Squares**
 - ◆ **Square Size**
 - ◆ **Threshold for each Square**

- **Using Threshold**
 - ◆ **By Square**
 - ◆ **By Interpolation**
 - ◆ **Overlapping Squares**

- **Variation Lightning Evaluation**

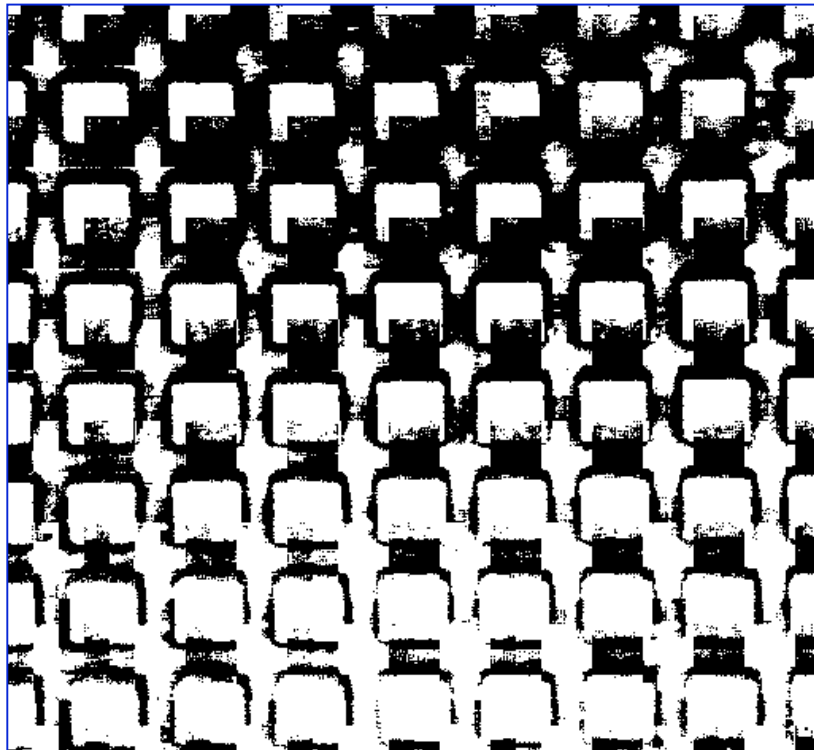


Otsu: Threshold at 188

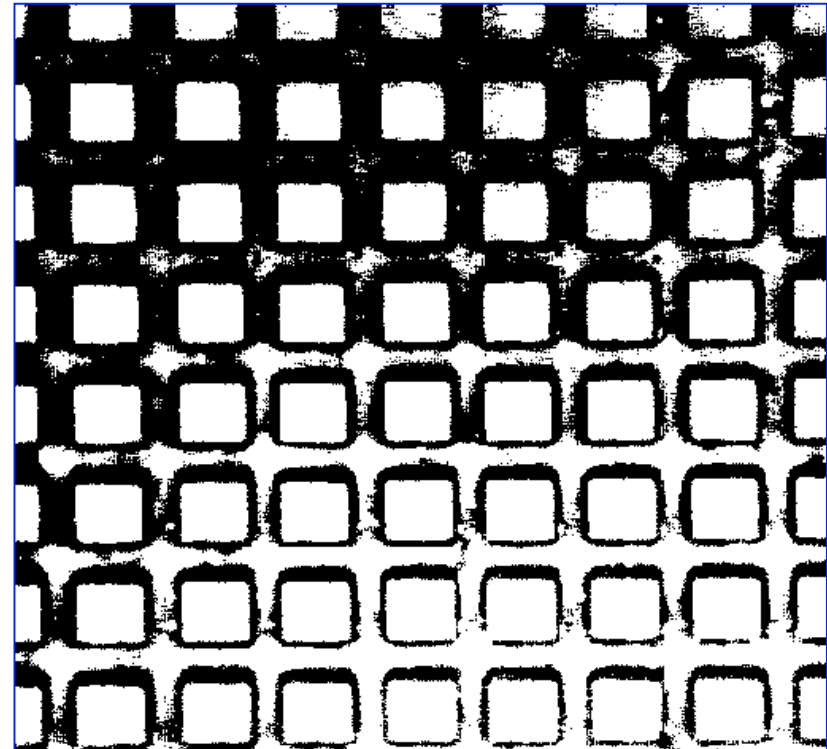


Otsu: 32x32 Squares

Otsu Method in each Square

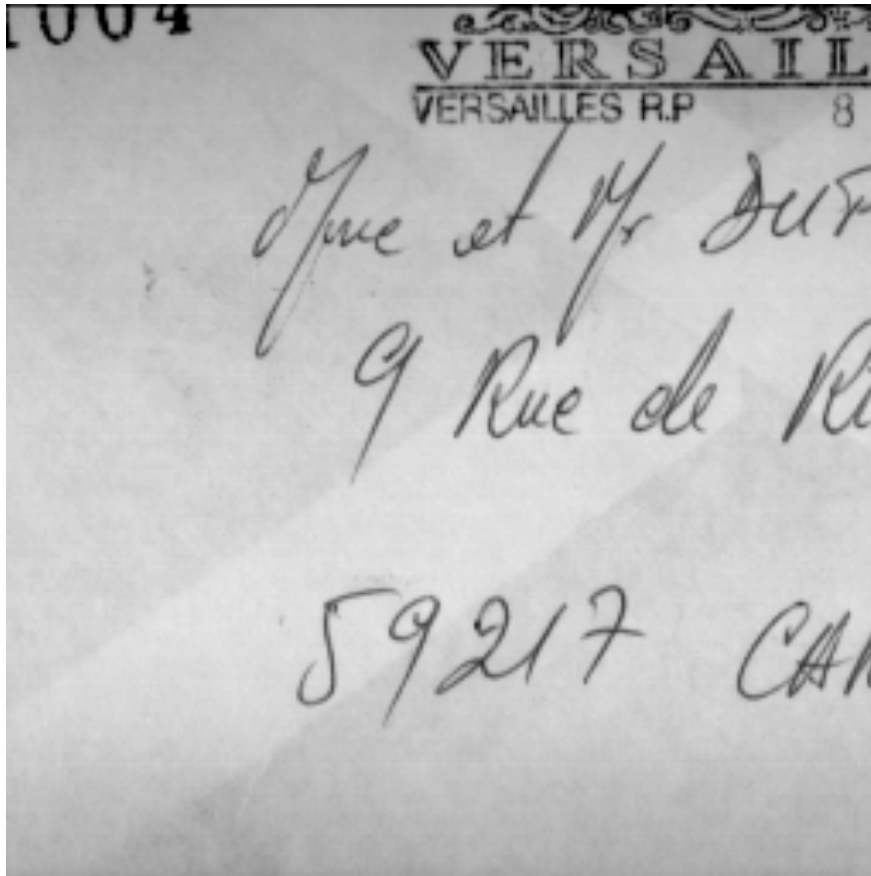


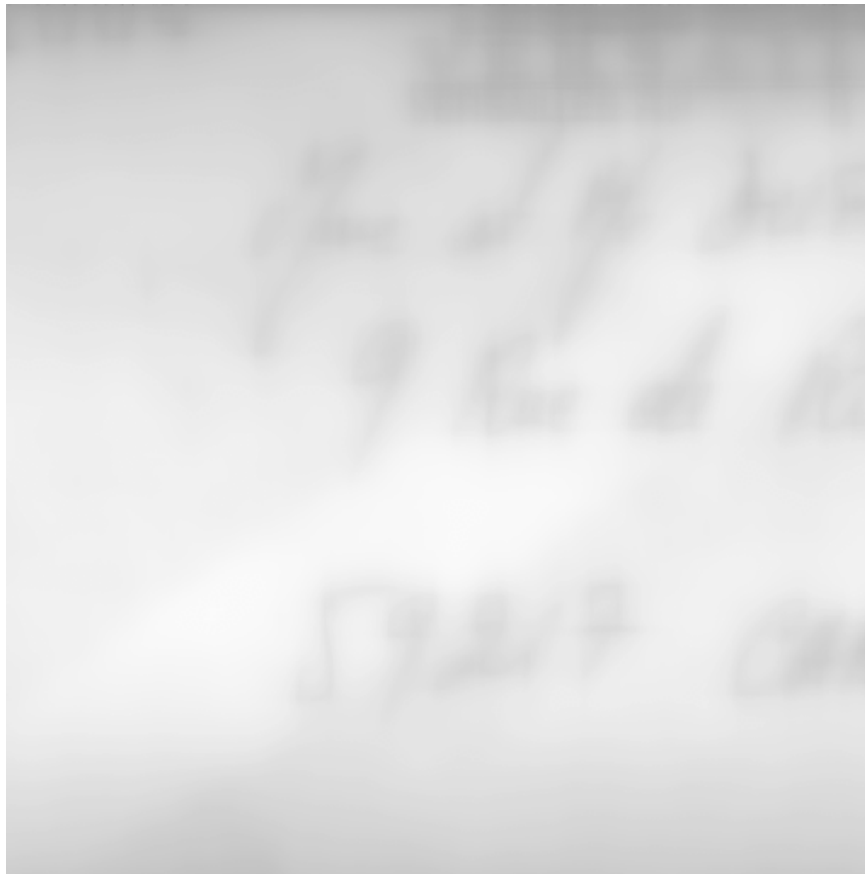
16x16 Square, too small

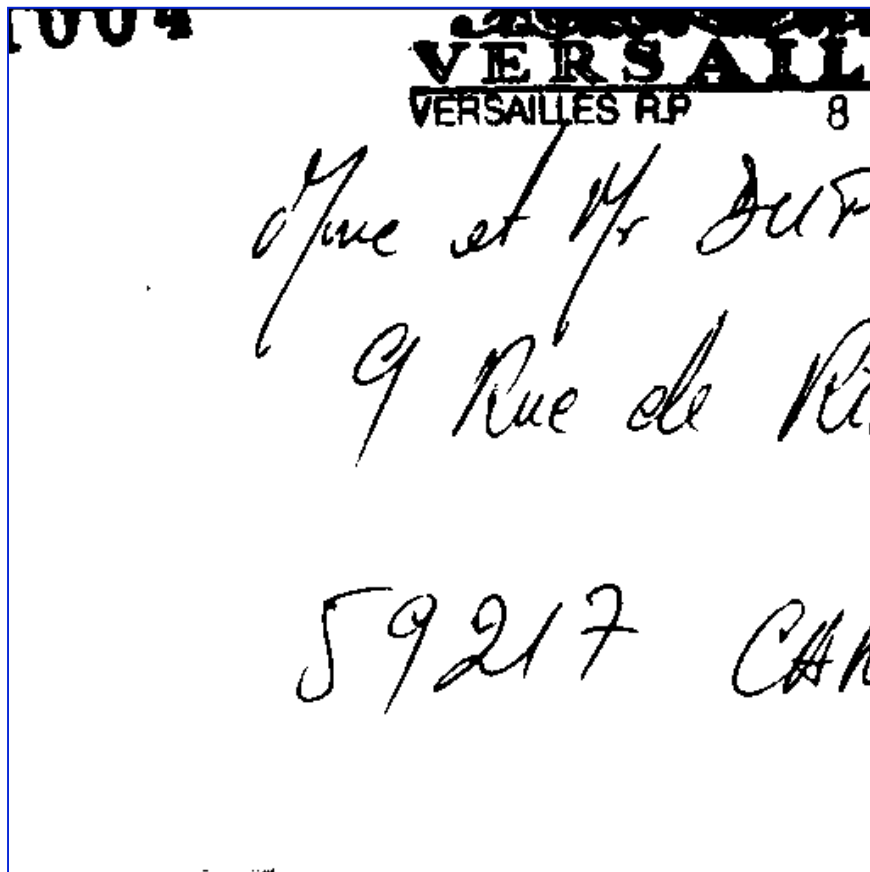


64x64 Square, good fit

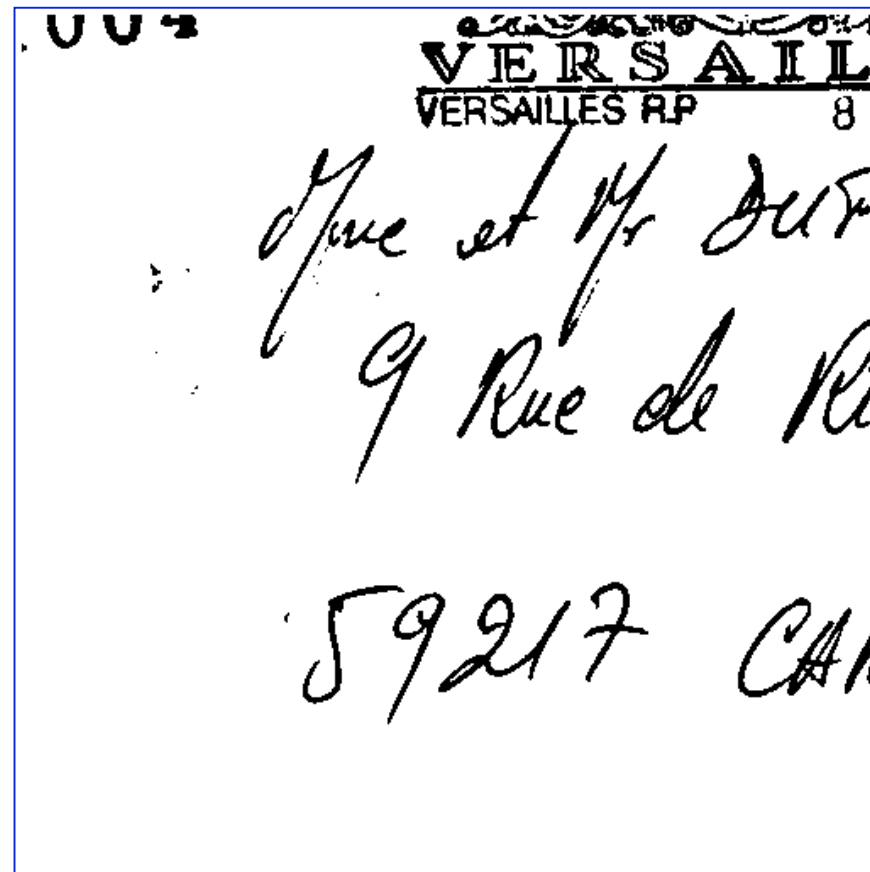
■ Variation Lightning Evaluation



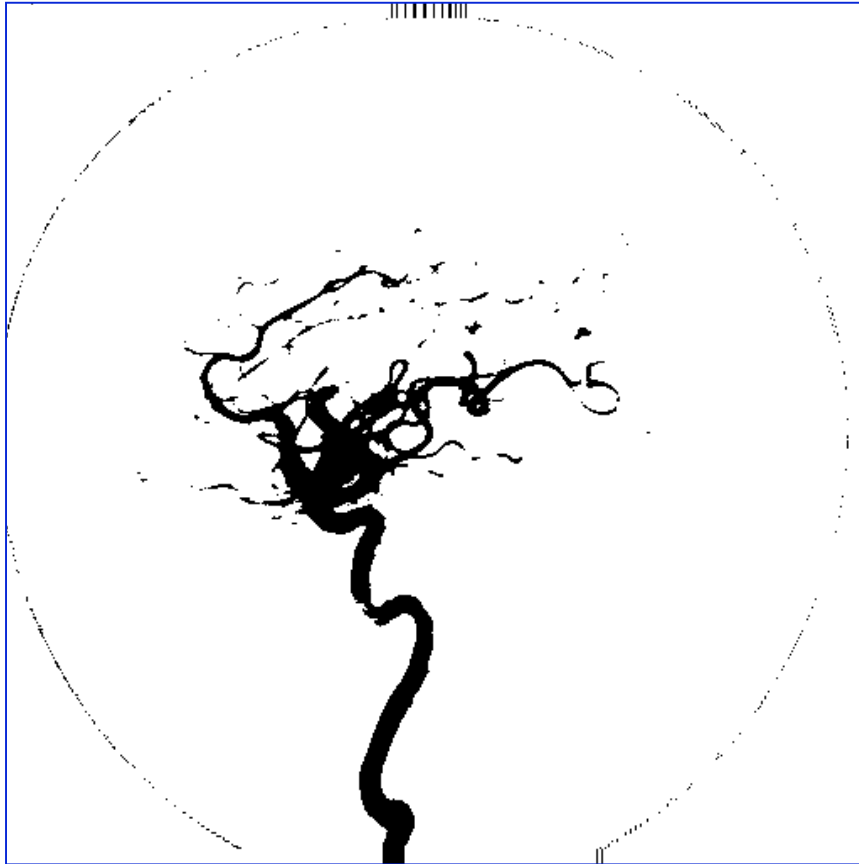




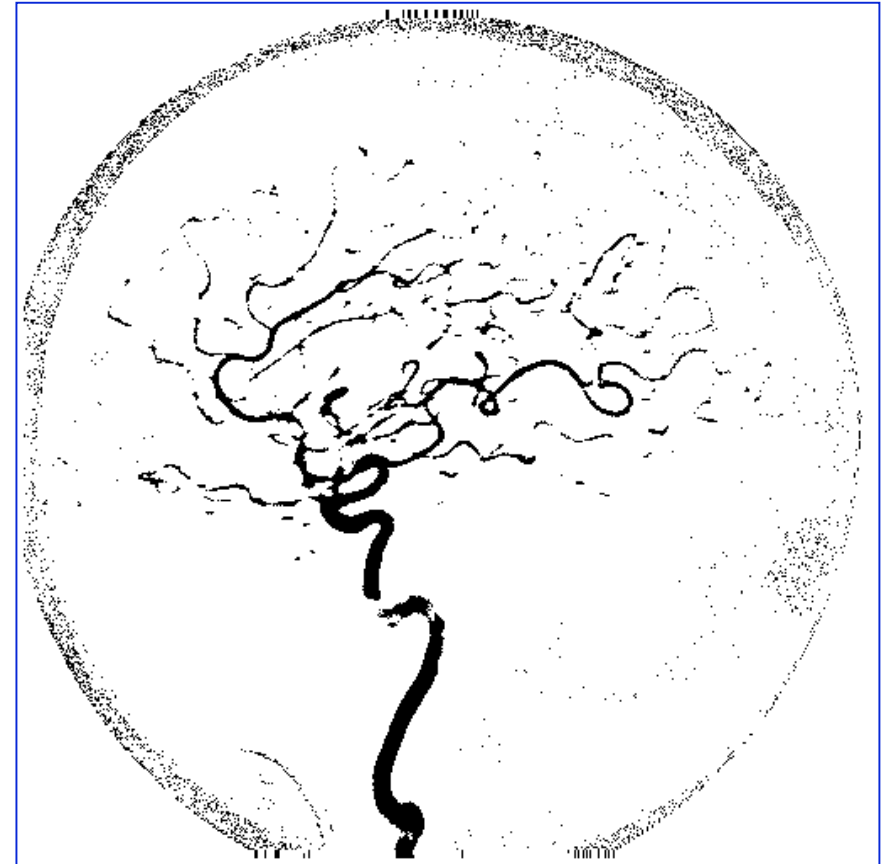
Otsu : seuil à 188



Filtrage passe-bas,
contraste de 10



Otsu : seuil à 109



Filtrage passe-bas,
contraste de 3